



The Parma Polyhedra Library
C Language Interface
User's Manual*
(version 1.2)

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Contents

1	Main Page	1
2	GNU General Public License	2
3	GNU Free Documentation License	10
4	Module Index	15
4.1	Modules	15
5	Class Index	15
5.1	Class List	15
6	Module Documentation	17
6.1	C Language Interface	17
6.2	Library Initialization and Finalization	18
6.3	Version Checking	19
6.4	Error Handling	20
6.5	Timeout Handling	22
6.6	Library Datatypes	24
7	Class Documentation	31
7.1	ppl_Artificial_Parameter_Sequence_const_iterator_tag Interface Reference	31
7.2	ppl_Artificial_Parameter_tag Interface Reference	31
7.3	ppl_Coefficient_tag Interface Reference	32
7.4	ppl_Congruence_System_const_iterator_tag Interface Reference	33
7.5	ppl_Congruence_System_tag Interface Reference	34
7.6	ppl_Congruence_tag Interface Reference	36
7.7	ppl_Constraint_System_const_iterator_tag Interface Reference	37
7.8	ppl_Constraint_System_tag Interface Reference	37
7.9	ppl_Constraint_tag Interface Reference	39
7.10	ppl_Generator_System_const_iterator_tag Interface Reference	40
7.11	ppl_Generator_System_tag Interface Reference	41
7.12	ppl_Generator_tag Interface Reference	42
7.13	ppl_Grid_Generator_System_const_iterator_tag Interface Reference	43
7.14	ppl_Grid_Generator_System_tag Interface Reference	44
7.15	ppl_Grid_Generator_tag Interface Reference	46
7.16	ppl_Linear_Expression_tag Interface Reference	47
7.17	ppl_MIP_Problem_tag Interface Reference	49
7.18	ppl_PIP_Decision_Node_tag Interface Reference	53
7.19	ppl_PIP_Problem_tag Interface Reference	54
7.20	ppl_PIP_Solution_Node_tag Interface Reference	57
7.21	ppl_PIP_Tree_Node_tag Interface Reference	58
7.22	ppl_Pointset_Powerset_C_Polyhedron_const_iterator_tag Interface Reference	59
7.23	ppl_Pointset_Powerset_C_Polyhedron_iterator_tag Interface Reference	60
7.24	ppl_Pointset_Powerset_C_Polyhedron_tag Interface Reference	61
7.25	ppl_Polyhedron_tag Interface Reference	62
	Index	79



1 Main Page

All the declarations needed for using the PPL's C interface (preprocessor symbols, data types, variables and functions) are collected in the header file `ppl_c.h`. This file, which is designed to work with pre-ANSI and ANSI C compilers as well as C99 and C++ compilers, should be included, either directly or via some other header file, with the directive

```
#include <ppl_c.h>
```

If this directive does not work, then your compiler is unable to find the file `ppl_c.h`. So check that the library is installed (if it is not installed, you may want to make `install`, perhaps with root privileges) in the right place (if not you may want to reconfigure the library using the appropriate pathname for the `--prefix` option); and that your compiler knows where it is installed (if not you should add the path to the directory where `ppl_c.h` is located to the compiler's include file search path; this is usually done with the `-I` option).

The name space of the PPL's C interface is `PPL_*` for preprocessor symbols, enumeration values and variables; and `ppl_*` for data types and function names. The interface systematically uses *opaque data types* (generic pointers that completely hide the internal representations from the client code) and provides all required access functions. By using just the interface, the client code can exploit all the functionalities of the library yet avoid directly manipulating the library's data structures. The advantages are that (1) applications do not depend on the internals of the library (these may change from release to release), and (2) the interface invariants can be thoroughly checked (by the access functions).

Note

All functions taking as input argument an opaque pointer datatype assume that such an argument is actually *referring to a valid PPL object*. For instance, a function with an argument having type `ppl_MIP_Problem_t` will expect a valid `MIP_Problem` object, previously initialized by calling, e.g., `ppl_new_MIP_Problem`. If that is not the case (e.g., if a null pointer is passed in), the behavior is undefined.

The PPL's C interface is initialized by means of the `ppl_initialize` function. This function must be called *before using any other interface of the library*. The application can release the resources allocated by the library by calling the `ppl_finalize` function. After this function is called *no other interface of the library may be used* until the interface is re-initialized using `ppl_initialize`.

Any application using the PPL should make sure that only the intended version(s) of the library are ever used. The version used can be checked at compile-time thanks to the macros `PPL_VERSION_MAJOR`, `PPL_VERSION_MINOR`, `PPL_VERSION_REVISION` and `PPL_VERSION_BETA`, which give, respectively major, minor, revision and beta numbers of the PPL version. This is an example of their use:

```
#if PPL_VERSION_MAJOR == 0 && PPL_VERSION_MINOR < 6
# error "PPL version 0.6 or following is required"
#endif
```

Compile-time checking, however, is not normally enough, particularly in an environment where there is dynamic linking. Run-time checking can be performed by means of the functions `ppl_version_major`, `ppl_version_minor`, `ppl_version_revision`, and `ppl_version_beta`. The PPL's C interface also provides functions `ppl_version`, returning character string containing the full version number, and `ppl_banner`, returning a string that, in addition, provides (pointers to) other useful information for the library user.

All programs using the PPL's C interface must link with the following libraries: `libppl_c` (PPL's C interface), `libppl` (PPL's core), `libgmpxx` (GMP's C++ interface), and `libgmp` (GMP's library core). On most Unix-like systems, this is done by adding `-lppl_c`, `-lppl`, `-lgmpxx`, and `-lgmp` to the compiler's or linker's command line. For example:

```
gcc myprogram.o -lppl_c -lppl -lgmpxx -lgmp
```

If this does not work, it means that your compiler/linker is not finding the libraries where it expects. Again, this could be because you forgot to install the library or you installed it in a non-standard location. In the

latter case you will need to use the appropriate options (usually `-L`) and, if you use shared libraries, some sort of run-time path selection mechanisms. Consult your compiler's documentation for details. Notice that the PPL is built using `Libtool` and an application can exploit this fact to significantly simplify the linking phase. See `Libtool`'s documentation for details. Those working under Linux can find a lot of useful information on how to use program libraries (including static, shared, and dynamically loaded libraries) in the `Program Library HOWTO`.

For examples on how to use the functions provided by the C interface, you are referred to the directory `demos/ppl_lpsol/` in the source distribution. It contains a *Mixed Integer (Linear) Programming* solver written in C. In order to use this solver you will need to install `GLPK` (the GNU Linear Programming Kit): this is used to read linear programs in MPS format.

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4 Module Index

4.1 Modules

Here is a list of all modules:

C Language Interface	17
Library Initialization and Finalization	18
Version Checking	19
Error Handling	20
Timeout Handling	22
Library Datatypes	24

5 Class Index

5.1 Class List

Here are the classes, structs, unions and interfaces with brief descriptions:

ppl.Artificial_Parameter_Sequence_const_iterator_tag	
Types and functions for iterating on PIP artificial parameters	31
ppl.Artificial_Parameter_tag	
Types and functions for PIP artificial parameters	31
ppl.Coefficient_tag	
Types and functions for coefficients	32

ppl.Congruence_System_const_iterator_tag	Types and functions for iterating on congruence systems	33
ppl.Congruence_System_tag	Types and functions for congruence systems	34
ppl.Congruence_tag	Types and functions for congruences	36
ppl.Constraint_System_const_iterator_tag	Types and functions for iterating on constraint systems	37
ppl.Constraint_System_tag	Types and functions for constraint systems	37
ppl.Constraint_tag	Types and functions for constraints	39
ppl.Generator_System_const_iterator_tag	Types and functions for iterating on generator systems	40
ppl.Generator_System_tag	Types and functions for generator systems	41
ppl.Generator_tag	Types and functions for generators	42
ppl.Grid_Generator_System_const_iterator_tag	Types and functions for iterating on grid generator systems	43
ppl.Grid_Generator_System_tag	Types and functions for grid generator systems	44
ppl.Grid_Generator_tag	Types and functions for grid generators	46
ppl.Linear_Expression_tag	Types and functions for linear expressions	47
ppl.MIP_Problem_tag	Types and functions for MIP problems	49
ppl.PIP_Decision_Node_tag	Types and functions for PIP decision nodes	53
ppl.PIP_Problem_tag	Types and functions for PIP problems	54
ppl.PIP_Solution_Node_tag	Types and functions for PIP solution nodes	57
ppl.PIP_Tree_Node_tag	Types and functions for generic PIP tree nodes	58

ppl_Pointset_Powerset_C_Polyhedron_const_iterator_tag	Types and functions for iterating on the disjuncts of a const ppl_Pointset_Powerset_C_Polyhedron_tag	59
ppl_Pointset_Powerset_C_Polyhedron_iterator_tag	Types and functions for iterating on the disjuncts of a ppl_Pointset_Powerset_C_Polyhedron_tag	60
ppl_Pointset_Powerset_C_Polyhedron_tag	Types and functions for the Pointset_Powerset of C_Polyhedron objects	61
ppl_Polyhedron_tag	Types and functions for the domains of C and NNC convex polyhedra	62

6 Module Documentation

6.1 C Language Interface

The Parma Polyhedra Library comes equipped with an interface for the C language.

6.2 Library Initialization and Finalization

Functions

- `int ppl_initialize` (void)
Initializes the Parma Polyhedra Library. This function must be called before any other function.
- `int ppl_finalize` (void)
Finalizes the Parma Polyhedra Library. This function must be called after any other function.
- `int ppl_set_rounding_for_PPL` (void)
Sets the FPU rounding mode so that the PPL abstractions based on floating point numbers work correctly.
- `int ppl_restore_pre_PPL_rounding` (void)
Sets the FPU rounding mode as it was before initialization of the PPL.
- `int ppl_irrational_precision` (unsigned *p)
Writes to p the precision parameter used for irrational calculations.
- `int ppl_set_irrational_precision` (unsigned p)
Sets the precision parameter used for irrational calculations.

6.2.1 Detailed Description

Functions for initialization/finalization of the library, as well as setting/resetting of floating-point rounding mode.

6.2.2 Function Documentation

int ppl_initialize (void) Initializes the Parma Polyhedra Library. This function must be called before any other function.

Returns

PPL_ERROR_INVALID_ARGUMENT if the library was already initialized.

int ppl_finalize (void) Finalizes the Parma Polyhedra Library. This function must be called after any other function.

Returns

PPL_ERROR_INVALID_ARGUMENT if the library was already finalized.

int ppl_set_rounding_for_PPL (void) Sets the FPU rounding mode so that the PPL abstractions based on floating point numbers work correctly.

This is performed automatically at initialization-time. Calling this function is needed only if `restore_pre_PPL_rounding()` has been previously called.

int ppl_restore_pre_PPL_rounding (void) Sets the FPU rounding mode as it was before initialization of the PPL.

After calling this function it is absolutely necessary to call `set_rounding_for_PPL()` before using any PPL abstractions based on floating point numbers. This is performed automatically at finalization-time.

int ppl_set_irrational_precision (unsigned p) Sets the precision parameter used for irrational calculations.

If `p` is less than or equal to `INT_MAX`, sets the precision parameter used for irrational calculations to `p`. Then, in the irrational calculations returning an unbounded rational, (e.g., when computing a square root), the lesser between numerator and denominator will be limited to 2^{**p} .

6.3 Version Checking

Macros

- `#define PPL_VERSION "1.2"`
A string containing the PPL version.
- `#define PPL_VERSION_MAJOR 1`
The major number of the PPL version.
- `#define PPL_VERSION_MINOR 2`
The minor number of the PPL version.
- `#define PPL_VERSION_REVISION 0`
The revision number of the PPL version.
- `#define PPL_VERSION_BETA 0`
The beta number of the PPL version. This is zero for official releases and nonzero for development snapshots.

Functions

- `int ppl_version_major (void)`
Returns the major number of the PPL version.
- `int ppl_version_minor (void)`
Returns the minor number of the PPL version.
- `int ppl_version_revision (void)`
Returns the revision number of the PPL version.
- `int ppl_version_beta (void)`
Returns the beta number of the PPL version.
- `int ppl_version (const char **p)`
*Writes to *p a pointer to a character string containing the PPL version.*
- `int ppl_banner (const char **p)`
*Writes to *p a pointer to a character string containing the PPL banner.*

6.3.1 Detailed Description

Symbolic constants and functions related to library version checking.

6.3.2 Macro Definition Documentation

#define PPL_VERSION "1.2" A string containing the PPL version.

Let M and m denote the numbers associated to `PPL_VERSION_MAJOR` and `PPL_VERSION_MINOR`, respectively. The format of `PPL_VERSION` is M "." m if both `PPL_VERSION_REVISION` (r) and `PPL_VERSION_BETA` (b) are zero, M "." m "pre" b if `PPL_VERSION_REVISION` is zero and `PPL_VERSION_BETA` is not zero, M "." m "." r if `PPL_VERSION_REVISION` is not zero and `PPL_VERSION_BETA` is zero, M "." m "." r "pre" b if neither `PPL_VERSION_REVISION` nor `PPL_VERSION_BETA` are zero.

6.3.3 Function Documentation

int ppl_banner (const char ** p) Writes to *p a pointer to a character string containing the PPL banner.

The banner provides information about the PPL version, the licensing, the lack of any warranty whatsoever, the C++ compiler used to build the library, where to report bugs and where to look for further information.

6.4 Error Handling

Enumerations

- `enum ppl_enum_error_code` {
PPL_ERROR_OUT_OF_MEMORY, PPL_ERROR_INVALID_ARGUMENT, PPL_ERROR_DOMAIN_ERROR, PPL_ERROR_LENGTH_ERROR,
PPL_ARITHMETIC_OVERFLOW, PPL_STDIO_ERROR, PPL_ERROR_INTERNAL_ERROR, PPL_ERROR_UNKNOWN_STANDARD_EXCEPTION,
PPL_ERROR_UNEXPECTED_ERROR, PPL_TIMEOUT_EXCEPTION, PPL_ERROR_LOGIC_ERROR }

Defines the error codes that any function may return.

Functions

- `int ppl_set_error_handler` (void(*h)(enum `ppl_enum_error_code` code, const char *description))
Installs the user-defined error handler pointed at by h.

6.4.1 Detailed Description

Symbolic constants and functions related to error reporting/handling.

6.4.2 Enumeration Type Documentation

`enum ppl_enum_error_code` Defines the error codes that any function may return.

Enumerator

PPL_ERROR_OUT_OF_MEMORY The virtual memory available to the process has been exhausted.

PPL_ERROR_INVALID_ARGUMENT A function has been invoked with an invalid argument.

PPL_ERROR_DOMAIN_ERROR A function has been invoked outside its domain of definition.

PPL_ERROR_LENGTH_ERROR The construction of an object that would exceed its maximum permitted size was attempted.

PPL_ARITHMETIC_OVERFLOW An arithmetic overflow occurred and the computation was consequently interrupted. This can *only* happen in library's incarnations using bounded integers as coefficients.

PPL_STDIO_ERROR An error occurred during a C input/output operation. A more precise indication of what went wrong is available via `errno`.

PPL_ERROR_INTERNAL_ERROR An internal error that was diagnosed by the PPL itself. This indicates a bug in the PPL.

PPL_ERROR_UNKNOWN_STANDARD_EXCEPTION A standard exception has been raised by the C++ run-time environment. This indicates a bug in the PPL.

PPL_ERROR_UNEXPECTED_ERROR A totally unknown, totally unexpected error happened. This indicates a bug in the PPL.

PPL_TIMEOUT_EXCEPTION An exception has been raised by the PPL as a timeout previously set by the user has expired.

PPL_ERROR_LOGIC_ERROR The client program attempted to use the PPL in a way that violates its internal logic. This happens, for instance, when the client attempts to use the timeout facilities on a system that does not support them.

6.4.3 Function Documentation

int ppl_set_error_handler (void(*)(enum ppl_enum_error_code code, const char *description) h)

Installs the user-defined error handler pointed at by *h*.

The error handler takes an error code and a textual description that gives further information about the actual error. The C string containing the textual description is read-only and its existence is not guaranteed after the handler has returned.

6.5 Timeout Handling

Functions

- `int ppl_set_timeout` (unsigned csecs)
Sets the timeout for computations whose completion could require an exponential amount of time.
- `int ppl_reset_timeout` (void)
Resets the timeout time so that the computation is not interrupted.
- `int ppl_set_deterministic_timeout` (unsigned long unscaled_weight, unsigned scale)
Sets a threshold for computations whose completion could require an exponential amount of time.
- `int ppl_reset_deterministic_timeout` (void)
Resets the deterministic timeout so that the computation is not interrupted.

6.5.1 Detailed Description

Functions for setting and resetting timeouts.

6.5.2 Function Documentation

`int ppl_set_timeout` (unsigned csecs) Sets the timeout for computations whose completion could require an exponential amount of time.

Parameters

<i>csecs</i>	The number of centiseconds sometimes after which a timeout will occur; it must be strictly greater than zero.
--------------	---

Computations taking exponential time will be interrupted some time after `csecs` centiseconds have elapsed since the call to the timeout setting function. If the computation is interrupted that way, the interrupted function will return error code `PPL_TIMEOUT_EXCEPTION`. Otherwise, if the computation completes without being interrupted, then the timeout should be reset by calling `ppl_reset_timeout()`.

`int ppl_set_deterministic_timeout` (unsigned long unscaled_weight, unsigned scale) Sets a threshold for computations whose completion could require an exponential amount of time.

Returns

`PPL_ERROR_INVALID_ARGUMENT` if `unscaled_weight` is zero or if the computed weight threshold exceeds the maximum allowed value.

Parameters

<i>unscaled_weight</i>	The unscaled maximum computational weight; it has to be non-zero.
<i>scale</i>	The scaling factor to be applied to <code>unscaled_weight</code> .

If `unscaled_weight` has value u and `scale` has value s , then the (scaled) weight threshold is computed as $w = u \cdot 2^s$. Computations taking exponential time will be interrupted some time after reaching the complexity threshold w . If the computation is interrupted that way, the interrupted function will return error code `PPL_TIMEOUT_EXCEPTION`. Otherwise, if the computation completes without being interrupted, then the deterministic timeout should be reset by calling `ppl_reset_deterministic_timeout()`.

Note

This "timeout" checking functionality is said to be *deterministic* because it is not based on actual elapsed time. Its behavior will only depend on (some of the) computations performed in the PPL library and it will be otherwise independent from the computation environment (CPU, operating system, compiler, etc.).

Warning

The weight mechanism is under beta testing. In particular, there is still no clear relation between the weight threshold and the actual computational complexity. As a consequence, client applications should be ready to reconsider the tuning of these weight thresholds when upgrading to newer version of the PPL.

6.6 Library Datatypes

Typedefs for the library datatypes and related symbolic constants.

Typedefs

- typedef size_t [ppl_dimension_type](#)
An unsigned integral type for representing space dimensions.
- typedef const char * [ppl_io_variable_output_function_type](#)([ppl_dimension_type](#) var)
The type of output functions used for printing variables.
- typedef struct [ppl_Coefficient_tag](#) * [ppl_Coefficient_t](#)
Opaque pointer.
- typedef struct [ppl_Coefficient_tag](#) const * [ppl_const_Coefficient_t](#)
Opaque pointer to const object.
- typedef struct [ppl_Linear_Expression_tag](#) * [ppl_Linear_Expression_t](#)
Opaque pointer.
- typedef struct [ppl_Linear_Expression_tag](#) const * [ppl_const_Linear_Expression_t](#)
Opaque pointer to const object.
- typedef struct [ppl_Constraint_tag](#) * [ppl_Constraint_t](#)
Opaque pointer.
- typedef struct [ppl_Constraint_tag](#) const * [ppl_const_Constraint_t](#)
Opaque pointer to const object.
- typedef struct [ppl_Constraint_System_tag](#) * [ppl_Constraint_System_t](#)
Opaque pointer.
- typedef struct [ppl_Constraint_System_tag](#) const * [ppl_const_Constraint_System_t](#)
Opaque pointer to const object.
- typedef struct [ppl_Constraint_System_const_iterator_tag](#) * [ppl_Constraint_System_const_iterator_t](#)
Opaque pointer.
- typedef struct [ppl_Constraint_System_const_iterator_tag](#) const * [ppl_const_Constraint_System_const_iterator_t](#)
Opaque pointer to const object.
- typedef struct [ppl_Generator_tag](#) * [ppl_Generator_t](#)
Opaque pointer.
- typedef struct [ppl_Generator_tag](#) const * [ppl_const_Generator_t](#)
Opaque pointer to const object.
- typedef struct [ppl_Generator_System_tag](#) * [ppl_Generator_System_t](#)
Opaque pointer.
- typedef struct [ppl_Generator_System_tag](#) const * [ppl_const_Generator_System_t](#)
Opaque pointer to const object.
- typedef struct [ppl_Generator_System_const_iterator_tag](#) * [ppl_Generator_System_const_iterator_t](#)
Opaque pointer.
- typedef struct [ppl_Generator_System_const_iterator_tag](#) const * [ppl_const_Generator_System_const_iterator_t](#)
Opaque pointer to const object.
- typedef struct [ppl_Congruence_tag](#) * [ppl_Congruence_t](#)
Opaque pointer.
- typedef struct [ppl_Congruence_tag](#) const * [ppl_const_Congruence_t](#)
Opaque pointer to const object.

- typedef struct `ppl_Congruence_System_tag` * `ppl_Congruence_System_t`
Opaque pointer.
- typedef struct `ppl_Congruence_System_tag` const * `ppl_const_Congruence_System_t`
Opaque pointer to const object.
- typedef struct `ppl_Congruence_System_const_iterator_tag` * `ppl_Congruence_System_const_iterator_t`
Opaque pointer.
- typedef struct `ppl_Congruence_System_const_iterator_tag` const * `ppl_const_Congruence_System_const_iterator_t`
Opaque pointer to const object.
- typedef struct `ppl_Grid_Generator_tag` * `ppl_Grid_Generator_t`
Opaque pointer.
- typedef struct `ppl_Grid_Generator_tag` const * `ppl_const_Grid_Generator_t`
Opaque pointer to const object.
- typedef struct `ppl_Grid_Generator_System_tag` * `ppl_Grid_Generator_System_t`
Opaque pointer.
- typedef struct `ppl_Grid_Generator_System_tag` const * `ppl_const_Grid_Generator_System_t`
Opaque pointer to const object.
- typedef struct `ppl_Grid_Generator_System_const_iterator_tag` * `ppl_Grid_Generator_System_const_iterator_t`
Opaque pointer.
- typedef struct `ppl_Grid_Generator_System_const_iterator_tag` const * `ppl_const_Grid_Generator_System_const_iterator_t`
Opaque pointer to const object.
- typedef struct `ppl_MIP_Problem_tag` * `ppl_MIP_Problem_t`
Opaque pointer.
- typedef struct `ppl_MIP_Problem_tag` const * `ppl_const_MIP_Problem_t`
Opaque pointer to const object.
- typedef struct `ppl_PIP_Problem_tag` * `ppl_PIP_Problem_t`
Opaque pointer.
- typedef struct `ppl_PIP_Problem_tag` const * `ppl_const_PIP_Problem_t`
Opaque pointer to const object.
- typedef struct `ppl_PIP_Tree_Node_tag` * `ppl_PIP_Tree_Node_t`
Opaque pointer.
- typedef struct `ppl_PIP_Tree_Node_tag` const * `ppl_const_PIP_Tree_Node_t`
Opaque pointer to const object.
- typedef struct `ppl_PIP_Decision_Node_tag` * `ppl_PIP_Decision_Node_t`
Opaque pointer.
- typedef struct `ppl_PIP_Decision_Node_tag` const * `ppl_const_PIP_Decision_Node_t`
Opaque pointer to const object.
- typedef struct `ppl_PIP_Solution_Node_tag` * `ppl_PIP_Solution_Node_t`
Opaque pointer.
- typedef struct `ppl_PIP_Solution_Node_tag` const * `ppl_const_PIP_Solution_Node_t`
Opaque pointer to const object.
- typedef struct `ppl_Artificial_Parameter_tag` * `ppl_Artificial_Parameter_t`
Opaque pointer.
- typedef struct `ppl_Artificial_Parameter_tag` const * `ppl_const_Artificial_Parameter_t`

- Opaque pointer to const object.*

 - typedef struct ppl_Artificial_Parameter_Sequence_tag * ppl_Artificial_Parameter_Sequence_t

Opaque pointer.
- typedef struct ppl_Artificial_Parameter_Sequence_tag const * ppl_const_Artificial_Parameter_Sequence_t

Opaque pointer to const object.
- typedef struct ppl_Artificial_Parameter_Sequence_const_iterator_tag * ppl_Artificial_Parameter_Sequence_const_iterator_t

Opaque pointer.
- typedef struct ppl_Artificial_Parameter_Sequence_const_iterator_tag const * ppl_const_Artificial_Parameter_Sequence_const_iterator_t

Opaque pointer to const object.
- typedef struct ppl_Polyhedron_tag * ppl_Polyhedron_t

Opaque pointer.
- typedef struct ppl_Polyhedron_tag const * ppl_const_Polyhedron_t

Opaque pointer to const object.
- typedef struct ppl_Pointset_Powerset_C_Polyhedron_tag * ppl_Pointset_Powerset_C_Polyhedron_t

Opaque pointer.
- typedef struct ppl_Pointset_Powerset_C_Polyhedron_tag const * ppl_const_Pointset_Powerset_C_Polyhedron_t

Opaque pointer to const object.
- typedef struct ppl_Pointset_Powerset_C_Polyhedron_iterator_tag * ppl_Pointset_Powerset_C_Polyhedron_iterator_t

Opaque pointer.
- typedef struct ppl_Pointset_Powerset_C_Polyhedron_iterator_tag const * ppl_const_Pointset_Powerset_C_Polyhedron_iterator_t

Opaque pointer to const object.
- typedef struct ppl_Pointset_Powerset_C_Polyhedron_const_iterator_tag * ppl_Pointset_Powerset_C_Polyhedron_const_iterator_t

Opaque pointer.
- typedef struct ppl_Pointset_Powerset_C_Polyhedron_const_iterator_tag const * ppl_const_Pointset_Powerset_C_Polyhedron_const_iterator_t

Opaque pointer to const object.

Enumerations

- enum ppl_enum_Constraint_Type { PPL_CONSTRAINT_TYPE_LESS_THAN, PPL_CONSTRAINT_TYPE_LESS_OR_EQUAL, PPL_CONSTRAINT_TYPE_EQUAL, PPL_CONSTRAINT_TYPE_GREATER_OR_EQUAL, PPL_CONSTRAINT_TYPE_GREATER_THAN }

Describes the relations represented by a constraint.
- enum ppl_enum_Generator_Type { PPL_GENERATOR_TYPE_LINE, PPL_GENERATOR_TYPE_RAY, PPL_GENERATOR_TYPE_POINT, PPL_GENERATOR_TYPE_CLOSURE_POINT }

Describes the different kinds of generators.
- enum ppl_enum_Grid_Generator_Type { PPL_GRID_GENERATOR_TYPE_LINE, PPL_GRID_GENERATOR_TYPE_PARAMETER, PPL_GRID_GENERATOR_TYPE_POINT }

Describes the different kinds of grid generators.
- enum ppl_enum_Bounded_Integer_Type_Width { PPL_BITS_8, PPL_BITS_16, PPL_BITS_32, PPL_BITS_64, PPL_BITS_128 }

Widths of bounded integer types.

- enum `ppl_enum_Bounded_Integer_Type_Representation` { `PPL_UNSIGNED`, `PPL_SIGNED_2_COMPLEMENT` }

Representation of bounded integer types.

- enum `ppl_enum_Bounded_Integer_Type_Overflow` { `PPL_OVERFLOW_WRAPS`, `PPL_OVERFLOW_UNDEFINED`, `PPL_OVERFLOW_IMPOSSIBLE` }

Overflow behavior of bounded integer types.

Functions

- int `ppl_max_space_dimension` (`ppl_dimension_type *m`)
Writes to `m` the maximum space dimension this library can handle.
- int `ppl_not_a_dimension` (`ppl_dimension_type *m`)
Writes to `m` a value that does not designate a valid dimension.
- int `ppl_io_print_variable` (`ppl_dimension_type var`)
Pretty-prints `var` to `stdout`.
- int `ppl_io_fprint_variable` (`FILE *stream`, `ppl_dimension_type var`)
Pretty-prints `var` to the given output `stream`.
- int `ppl_io_asprint_variable` (`char **strp`, `ppl_dimension_type var`)
Pretty-prints `var` to a malloc-allocated string, a pointer to which is returned via `strp`.
- int `ppl_io_set_variable_output_function` (`ppl_io_variable_output_function_type *p`)
Sets the output function to be used for printing variables to `p`.
- int `ppl_io_get_variable_output_function` (`ppl_io_variable_output_function_type **pp`)
Writes a pointer to the current variable output function to `pp`.
- char * `ppl_io_wrap_string` (`const char *src`, unsigned `indent_depth`, unsigned `preferred_first_line_length`, unsigned `preferred_line_length`)
Utility function for the wrapping of lines of text.

Variables

- unsigned int `PPL_COMPLEXITY_CLASS_POLYNOMIAL`
Code of the worst-case polynomial complexity class.
- unsigned int `PPL_COMPLEXITY_CLASS_SIMPLEX`
Code of the worst-case exponential but typically polynomial complexity class.
- unsigned int `PPL_COMPLEXITY_CLASS_ANY`
Code of the universal complexity class.
- unsigned int `PPL_POLY_CON_RELATION_IS_DISJOINT`
Individual bit saying that the polyhedron and the set of points satisfying the constraint are disjoint.
- unsigned int `PPL_POLY_CON_RELATION_STRICTLY_INTERSECTS`
Individual bit saying that the polyhedron intersects the set of points satisfying the constraint, but it is not included in it.
- unsigned int `PPL_POLY_CON_RELATION_IS_INCLUDED`
Individual bit saying that the polyhedron is included in the set of points satisfying the constraint.
- unsigned int `PPL_POLY_CON_RELATION_SATURATES`
Individual bit saying that the polyhedron is included in the set of points saturating the constraint.
- unsigned int `PPL_POLY_GEN_RELATION_SUBSUMES`
Individual bit saying that adding the generator would not change the polyhedron.

6.6.1 Detailed Description

Typedefs for the library datatypes and related symbolic constants.

The datatypes provided by the library should be manipulated by means of the corresponding opaque pointer types and the functions working on them.

Note

To simplify the detection of common programming mistakes, we provide both pointer-to-const and pointer-to-nonconst opaque pointers, with implicit conversions mapping each pointer-to-nonconst to the corresponding pointer-to-const when needed. The user of the C interface is therefore recommended to adopt the pointer-to-const type whenever read-only access is meant.

6.6.2 Typedef Documentation

typedef const char* ppl_io_variable_output_function_type(ppl_dimension_type var) The type of output functions used for printing variables.

An output function for variables must write a textual representation for `var` to a character buffer, null-terminate it, and return a pointer to the beginning of the buffer. In case the operation fails, 0 should be returned and perhaps `errno` should be set in a meaningful way. The library does nothing with the buffer, besides printing its contents.

6.6.3 Enumeration Type Documentation

enum ppl_enum_Constraint_Type Describes the relations represented by a constraint.

Enumerator

PPL_CONSTRAINT_TYPE_LESS_THAN The constraint is of the form $e < 0$.

PPL_CONSTRAINT_TYPE_LESS_OR_EQUAL The constraint is of the form $e \leq 0$.

PPL_CONSTRAINT_TYPE_EQUAL The constraint is of the form $e = 0$.

PPL_CONSTRAINT_TYPE_GREATER_OR_EQUAL The constraint is of the form $e \geq 0$.

PPL_CONSTRAINT_TYPE_GREATER_THAN The constraint is of the form $e > 0$.

enum ppl_enum_Generator_Type Describes the different kinds of generators.

Enumerator

PPL_GENERATOR_TYPE_LINE The generator is a line.

PPL_GENERATOR_TYPE_RAY The generator is a ray.

PPL_GENERATOR_TYPE_POINT The generator is a point.

PPL_GENERATOR_TYPE_CLOSURE_POINT The generator is a closure point.

enum ppl_enum_Grid_Generator_Type Describes the different kinds of grid generators.

Enumerator

PPL_GRID_GENERATOR_TYPE_LINE The grid generator is a line.

PPL_GRID_GENERATOR_TYPE_PARAMETER The grid generator is a parameter.

PPL_GRID_GENERATOR_TYPE_POINT The grid generator is a point.

enum ppl_enum_Bounded_Integer_Type_Width Widths of bounded integer types.

Enumerator

- PPL_BITS_8** 8 bits.
- PPL_BITS_16** 16 bits.
- PPL_BITS_32** 32 bits.
- PPL_BITS_64** 64 bits.
- PPL_BITS_128** 128 bits.

enum ppl_enum_Bounded_Integer_Type_Representation Representation of bounded integer types.

Enumerator

- PPL_UNSIGNED** Unsigned binary.
- PPL_SIGNED_2_COMPLEMENT** Signed binary where negative values are represented by the two's complement of the absolute value.

enum ppl_enum_Bounded_Integer_Type_Overflow Overflow behavior of bounded integer types.

Enumerator

- PPL_OVERFLOW_WRAPS** On overflow, wrapping takes place. This means that, for a w -bit bounded integer, the computation happens modulo 2^w .
- PPL_OVERFLOW_UNDEFINED** On overflow, the result is undefined. This simply means that the result of the operation resulting in an overflow can take any value.

Note

Even though something more serious can happen in the system being analyzed—due to, e.g., C's undefined behavior—, here we are only concerned with the results of arithmetic operations. It is the responsibility of the analyzer to ensure that other manifestations of undefined behavior are conservatively approximated.

- PPL_OVERFLOW_IMPOSSIBLE** Overflow is impossible. This is for the analysis of languages where overflow is trapped before it affects the state, for which, thus, any indication that an overflow may have affected the state is necessarily due to the imprecision of the analysis.

6.6.4 Function Documentation

char* ppl_io_wrap_string (const char * src, unsigned indent_depth, unsigned preferred_first_line_length, unsigned preferred_line_length) Utility function for the wrapping of lines of text.

Parameters

<i>src</i>	The source string holding the text to wrap.
<i>indent_depth</i>	The indentation depth.
<i>preferred_first_line_length</i>	The preferred length for the first line of text.

<i>preferred_↔ line_length</i>	The preferred length for all the lines but the first one.
------------------------------------	---

Returns

The wrapped string in a malloc-allocated buffer.

7 Class Documentation

7.1 ppl_Artificial_Parameter_Sequence_const_iterator_tag Interface Reference

Types and functions for iterating on PIP artificial parameters.

```
#include <ppl_c_header.h>
```

Related Functions

(Note that these are not member functions.)

Constructors, Assignment and Destructor

- `int ppl_new_Artificial_Parameter_Sequence_const_iterator (ppl_Artificial_Parameter_Sequence_const_iterator_t *papit)`
Builds a new 'const iterator' and writes a handle to it at address papit.
- `int ppl_new_Artificial_Parameter_Sequence_const_iterator_from_Artificial_Parameter_Sequence_const_iterator (ppl_Artificial_Parameter_Sequence_const_iterator_t *papit, ppl_const_Artificial_Parameter_Sequence_const_iterator_t apit)`
Builds a const iterator that is a copy of apit; writes a handle for the newly created const iterator at address papit.
- `int ppl_assign_Artificial_Parameter_Sequence_const_iterator_from_Artificial_Parameter_Sequence_const_iterator (ppl_Artificial_Parameter_Sequence_const_iterator_t dst, ppl_const_Artificial_Parameter_Sequence_const_iterator_t src)`
Assigns a copy of the const iterator src to dst.
- `int ppl_delete_Artificial_Parameter_Sequence_const_iterator (ppl_const_Artificial_Parameter_Sequence_const_iterator_t apit)`
Invalidates the handle apit: this makes sure the corresponding resources will eventually be released.

Dereferencing, Incrementing and Equality Testing

- `int ppl_Artificial_Parameter_Sequence_const_iterator_dereference (ppl_const_Artificial_Parameter_Sequence_const_iterator_t apit, ppl_const_Artificial_Parameter_t *pap)`
Dereference apit writing a const handle to the resulting artificial parameter at address pap.
- `int ppl_Artificial_Parameter_Sequence_const_iterator_increment (ppl_Artificial_Parameter_Sequence_const_iterator_t apit)`
Increment apit so that it "points" to the next artificial parameter.
- `int ppl_Artificial_Parameter_Sequence_const_iterator_equal_test (ppl_const_Artificial_Parameter_Sequence_const_iterator_t x, ppl_const_Artificial_Parameter_Sequence_const_iterator_t y)`
Returns a positive integer if the iterators corresponding to x and y are equal; returns 0 if they are different.

7.1.1 Detailed Description

Types and functions for iterating on PIP artificial parameters.

The documentation for this interface was generated from the following file:

- `ppl_c_header.h`

7.2 ppl_Artificial_Parameter_tag Interface Reference

Types and functions for PIP artificial parameters.

```
#include <ppl_c_header.h>
```

Related Functions

(Note that these are not member functions.)

- int `ppl_Artificial_Parameter_get_Linear_Expression` (`ppl_const_Artificial_Parameter_t ap`, `ppl_Linear_Expression_t le`)
Copies into `le` the linear expression in artificial parameter `ap`.
- int `ppl_Artificial_Parameter_coefficient` (`ppl_const_Artificial_Parameter_t ap`, `ppl_dimension_type var`, `ppl_Coefficient_t n`)
Copies into `n` the coefficient of variable `var` in the artificial parameter `ap`.
- int `ppl_Artificial_Parameter_get_inhomogeneous_term` (`ppl_const_Artificial_Parameter_t ap`, `ppl_Coefficient_t n`)
Copies into `n` the inhomogeneous term of the artificial parameter `ap`.
- int `ppl_Artificial_Parameter_denominator` (`ppl_const_Artificial_Parameter_t ap`, `ppl_Coefficient_t n`)
Copies into `n` the denominator in artificial parameter `ap`.

Input/Output Functions

- int `ppl_io_print_Artificial_Parameter` (`ppl_const_Artificial_Parameter_t x`)
Prints `x` to `stdout`.
- int `ppl_io_fprint_Artificial_Parameter` (`FILE *stream`, `ppl_const_Artificial_Parameter_t x`)
Prints `x` to the given output `stream`.
- int `ppl_io_asprint_Artificial_Parameter` (`char **strp`, `ppl_const_Artificial_Parameter_t x`)
Prints `x` to a malloc-allocated string, a pointer to which is returned via `strp`.
- int `ppl_Artificial_Parameter_ascii_dump` (`ppl_const_Artificial_Parameter_t x`, `FILE *stream`)
Dumps an ascii representation of `x` on `stream`.
- int `ppl_Artificial_Parameter_ascii_load` (`ppl_Artificial_Parameter_t x`, `FILE *stream`)
Loads an ascii representation of `x` from `stream`.

7.2.1 Detailed Description

Types and functions for PIP artificial parameters.

The types and functions for PIP artificial parameters provide an interface towards *Artificial_Parameter*. The documentation for this interface was generated from the following file:

- `ppl.c.header.h`

7.3 `ppl_Coefficient_tag` Interface Reference

Types and functions for coefficients.

```
#include <ppl.c.header.h>
```

Related Functions

(Note that these are not member functions.)

Constructors, Assignment and Destructor

- int `ppl_new_Coefficient` (`ppl_Coefficient_t *pc`)
Creates a new coefficient with value 0 and writes a handle for the newly created coefficient at address `pc`.
- int `ppl_new_Coefficient_from_mpz_t` (`ppl_Coefficient_t *pc`, `mpz_t z`)
Creates a new coefficient with the value given by the GMP integer `z` and writes a handle for the newly created coefficient at address `pc`.
- int `ppl_new_Coefficient_from_Coefficient` (`ppl_Coefficient_t *pc`, `ppl_const_Coefficient_t c`)

- *Builds a coefficient that is a copy of `c`; writes a handle for the newly created coefficient at address `pc`.*
- `int ppl_assign_Coefficient_from_mpz_t (ppl_Coefficient_t dst, mpz_t z)`
Assign to `dst` the value given by the GMP integer `z`.
- `int ppl_assign_Coefficient_from_Coefficient (ppl_Coefficient_t dst, ppl_const_Coefficient_t src)`
Assigns a copy of the coefficient `src` to `dst`.
- `int ppl_delete_Coefficient (ppl_const_Coefficient_t c)`
Invalidates the handle `c`: this makes sure the corresponding resources will eventually be released.

Read-Only Accessor Functions

- `int ppl_Coefficient_to_mpz_t (ppl_const_Coefficient_t c, mpz_t z)`
Sets the value of the GMP integer `z` to the value of `c`.
- `int ppl_Coefficient_OK (ppl_const_Coefficient_t c)`
Returns a positive integer if `c` is well formed, i.e., if it satisfies all its implementation invariants; returns 0 and perhaps makes some noise if `c` is broken. Useful for debugging purposes.
- `int ppl_Coefficient_is_bounded (void)`
Returns a positive integer if coefficients are bounded; returns 0 otherwise.
- `int ppl_Coefficient_min (mpz_t min)`
Returns a positive integer if coefficients are bounded, in which case `min` is set to their minimum value; returns 0 otherwise.
- `int ppl_Coefficient_max (mpz_t max)`
Returns a positive integer if coefficients are bounded, in which case `max` is set to their maximum value; returns 0 otherwise.

I/O Functions

- `int ppl_io_print_Coefficient (ppl_const_Coefficient_t x)`
Prints `x` to `stdout`.
- `int ppl_io_fprint_Coefficient (FILE *stream, ppl_const_Coefficient_t x)`
Prints `x` to the given output `stream`.
- `int ppl_io_asprint_Coefficient (char **strp, ppl_const_Coefficient_t x)`
Prints `x` to a malloc-allocated string, a pointer to which is returned via `strp`.

7.3.1 Detailed Description

Types and functions for coefficients.

The types and functions for coefficients provide an interface towards *Coefficient*. Depending on configuration, the PPL coefficients may be implemented by the unbounded precision integers provided by GMP (default), or by bounded precision integers (with checks for overflows).

The documentation for this interface was generated from the following file:

- `ppl.c.header.h`

7.4 `ppl_Congruence_System_const_iterator_tag` Interface Reference

Types and functions for iterating on congruence systems.

```
#include <ppl.c.header.h>
```

Related Functions

(Note that these are not member functions.)

Constructors, Assignment and Destructor

- `int ppl_new_Congruence_System_const_iterator (ppl_Congruence_System_const_iterator_t *pcit)`

- Builds a new 'const iterator' and writes a handle to it at address `pcit`.*

 - `int ppl_new_Congruence_System_const_iterator_from_Congruence_System_const_iterator (ppl_Congruence_System_const_iterator_t *pcit, ppl_const_Congruence_System_const_iterator_t cit)`

Builds a const iterator that is a copy of `cit`; writes a handle for the newly created const iterator at address `pcit`.
 - `int ppl_assign_Congruence_System_const_iterator_from_Congruence_System_const_iterator (ppl_Congruence_System_const_iterator_t dst, ppl_const_Congruence_System_const_iterator_t src)`

Assigns a copy of the const iterator `src` to `dst`.
 - `int ppl_delete_Congruence_System_const_iterator (ppl_const_Congruence_System_const_iterator_t cit)`

Invalidates the handle `cit`: this makes sure the corresponding resources will eventually be released.

Dereferencing, Incrementing and Equality Testing

- `int ppl_Congruence_System_const_iterator_dereference (ppl_const_Congruence_System_const_iterator_t cit, ppl_const_Congruence_t *pc)`

Dereference `cit` writing a const handle to the resulting congruence at address `pc`.
- `int ppl_Congruence_System_const_iterator_increment (ppl_Congruence_System_const_iterator_t cit)`

Increment `cit` so that it "points" to the next congruence.
- `int ppl_Congruence_System_const_iterator_equal_test (ppl_const_Congruence_System_const_iterator_t x, ppl_const_Congruence_System_const_iterator_t y)`

Returns a positive integer if the iterators corresponding to `x` and `y` are equal; returns 0 if they are different.

7.4.1 Detailed Description

Types and functions for iterating on congruence systems.

The types and functions for congruence systems iterators provide read-only access to the elements of a congruence system by interfacing `Congruence_System::const_iterator`.

The documentation for this interface was generated from the following file:

- `ppl_c_header.h`

7.5 `ppl_Congruence_System_tag` Interface Reference

Types and functions for congruence systems.

```
#include <ppl_c_header.h>
```

Related Functions

(Note that these are not member functions.)

Constructors, Assignment and Destructor

- `int ppl_new_Congruence_System (ppl_Congruence_System_t *pcs)`

Builds an empty system of congruences and writes a handle to it at address `pcs`.
- `int ppl_new_Congruence_System_zero_dim_empty (ppl_Congruence_System_t *pcs)`

Builds a zero-dimensional, unsatisfiable congruence system and writes a handle to it at address `pcs`.
- `int ppl_new_Congruence_System_from_Congruence (ppl_Congruence_System_t *pcs, ppl_const_Congruence_t c)`

Builds the singleton congruence system containing only a copy of congruence `c`; writes a handle for the newly created system at address `pcs`.
- `int ppl_new_Congruence_System_from_Congruence_System (ppl_Congruence_System_t *pcs, ppl_const_Congruence_System_t cs)`

Builds a congruence system that is a copy of `cs`; writes a handle for the newly created system at address `pcs`.

- `int ppl_assign_Congruence_System_from_Congruence_System (ppl_Congruence_System_t dst, ppl_const_Congruence_System_t src)`

Assigns a copy of the congruence system `src` to `dst`.

- `int ppl_delete_Congruence_System (ppl_const_Congruence_System_t cs)`

Invalidates the handle `cs`: this makes sure the corresponding resources will eventually be released.

Functions that Do Not Modify the Congruence System

- `int ppl_Congruence_System_space_dimension (ppl_const_Congruence_System_t cs, ppl_dimension_type *m)`

Writes to `m` the dimension of the vector space enclosing `cs`.

- `int ppl_Congruence_System_empty (ppl_const_Congruence_System_t cs)`

Returns a positive integer if `cs` contains no (non-trivial) congruence; returns 0 otherwise.

- `int ppl_Congruence_System_begin (ppl_const_Congruence_System_t cs, ppl_Congruence_System_const_iterator_t cit)`

Assigns to `cit` a const iterator "pointing" to the beginning of the congruence system `cs`.

- `int ppl_Congruence_System_end (ppl_const_Congruence_System_t cs, ppl_Congruence_System_const_iterator_t cit)`

Assigns to `cit` a const iterator "pointing" past the end of the congruence system `cs`.

- `int ppl_Congruence_System_OK (ppl_const_Congruence_System_t cs)`

Returns a positive integer if `cs` is well formed, i.e., if it satisfies all its implementation invariants; returns 0 and perhaps makes some noise if `cs` is broken. Useful for debugging purposes.

Functions that May Modify the Congruence System

- `int ppl_Congruence_System_clear (ppl_Congruence_System_t cs)`

Removes all the congruences from the congruence system `cs` and sets its space dimension to 0.

- `int ppl_Congruence_System_insert_Congruence (ppl_Congruence_System_t cs, ppl_const_Congruence_t c)`

Inserts a copy of the congruence `c` into `cs`; the space dimension is increased, if necessary.

Input/Output Functions

- `int ppl_io_print_Congruence_System (ppl_const_Congruence_System_t x)`

Prints `x` to `stdout`.

- `int ppl_io_fprint_Congruence_System (FILE *stream, ppl_const_Congruence_System_t x)`

Prints `x` to the given output `stream`.

- `int ppl_io_asprint_Congruence_System (char **strp, ppl_const_Congruence_System_t x)`

Prints `x` to a malloc-allocated string, a pointer to which is returned via `strp`.

- `int ppl_Congruence_System_ascii_dump (ppl_const_Congruence_System_t x, FILE *stream)`

Dumps an ascii representation of `x` on `stream`.

- `int ppl_Congruence_System_ascii_load (ppl_Congruence_System_t x, FILE *stream)`

Loads an ascii representation of `x` from `stream`.

7.5.1 Detailed Description

Types and functions for congruence systems.

The types and functions for congruence systems provide an interface towards *Congruence_System*.

The documentation for this interface was generated from the following file:

- `ppl_c.header.h`

7.6 ppl_Congruence_tag Interface Reference

Types and functions for congruences.

```
#include <ppl_c_header.h>
```

Related Functions

(Note that these are not member functions.)

Constructors, Assignment and Destructor

- `int ppl_new_Congruence (ppl_Congruence_t *pc, ppl_const_Linear_Expression_t le, ppl_const_Coefficient_t m)`
Creates the new congruence $le = 0 \pmod{m}$ and writes a handle for it at address `pc`. The space dimension of the new congruence is equal to the space dimension of `le`.
- `int ppl_new_Congruence_zero_dim_false (ppl_Congruence_t *pc)`
Creates the unsatisfiable (zero-dimension space) congruence $0 = 1 \pmod{0}$ and writes a handle for it at address `pc`.
- `int ppl_new_Congruence_zero_dim_integrity (ppl_Congruence_t *pc)`
Creates the true (zero-dimension space) congruence $0 = 1 \pmod{1}$, also known as integrity congruence. A handle for the newly created congruence is written at address `pc`.
- `int ppl_new_Congruence_from_Congruence (ppl_Congruence_t *pc, ppl_const_Congruence_t c)`
Builds a congruence that is a copy of `c`; writes a handle for the newly created congruence at address `pc`.
- `int ppl_assign_Congruence_from_Congruence (ppl_Congruence_t dst, ppl_const_Congruence_t src)`
Assigns a copy of the congruence `src` to `dst`.
- `int ppl_delete_Congruence (ppl_const_Congruence_t c)`
Invalidates the handle `c`: this makes sure the corresponding resources will eventually be released.

Functions that Do Not Modify the Congruence

- `int ppl_Congruence_space_dimension (ppl_const_Congruence_t c, ppl_dimension_type *m)`
Writes to `m` the space dimension of `c`.
- `int ppl_Congruence_coefficient (ppl_const_Congruence_t c, ppl_dimension_type var, ppl_Coefficient_t n)`
Copies into `n` the coefficient of variable `var` in congruence `c`.
- `int ppl_Congruence_inhomogeneous_term (ppl_const_Congruence_t c, ppl_Coefficient_t n)`
Copies into `n` the inhomogeneous term of congruence `c`.
- `int ppl_Congruence_modulus (ppl_const_Congruence_t c, ppl_Coefficient_t m)`
Copies into `m` the modulus of congruence `c`.
- `int ppl_Congruence_OK (ppl_const_Congruence_t c)`
Returns a positive integer if `c` is well formed, i.e., if it satisfies all its implementation invariants; returns 0 and perhaps makes some noise if `c` is broken. Useful for debugging purposes.

Input/Output Functions

- `int ppl_io_print_Congruence (ppl_const_Congruence_t x)`
Prints `x` to `stdout`.
- `int ppl_io_fprint_Congruence (FILE *stream, ppl_const_Congruence_t x)`
Prints `x` to the given output `stream`.
- `int ppl_io_asprint_Congruence (char **strp, ppl_const_Congruence_t x)`
Prints `x` to a malloc-allocated string, a pointer to which is returned via `strp`.
- `int ppl_Congruence_ascii_dump (ppl_const_Congruence_t x, FILE *stream)`
Dumps an ascii representation of `x` on `stream`.
- `int ppl_Congruence_ascii_load (ppl_Congruence_t x, FILE *stream)`
Loads an ascii representation of `x` from `stream`.

7.6.1 Detailed Description

Types and functions for congruences.

The types and functions for congruences provide an interface towards *Congruence*.

The documentation for this interface was generated from the following file:

- `ppl_c.header.h`

7.7 `ppl_Constraint_System_const_iterator_tag` Interface Reference

Types and functions for iterating on constraint systems.

```
#include <ppl_c.header.h>
```

Related Functions

(Note that these are not member functions.)

Constructors, Assignment and Destructor

- `int ppl_new_Constraint_System_const_iterator (ppl_Constraint_System_const_iterator_t *pcit)`
Builds a new 'const iterator' and writes a handle to it at address `pcit`.
- `int ppl_new_Constraint_System_const_iterator_from_Constraint_System_const_iterator (ppl_Constraint_System_const_iterator_t *pcit, ppl_const_Constraint_System_const_iterator_t cit)`
Builds a const iterator that is a copy of `cit`; writes a handle for the newly created const iterator at address `pcit`.
- `int ppl_assign_Constraint_System_const_iterator_from_Constraint_System_const_iterator (ppl_Constraint_System_const_iterator_t dst, ppl_const_Constraint_System_const_iterator_t src)`
Assigns a copy of the const iterator `src` to `dst`.
- `int ppl_delete_Constraint_System_const_iterator (ppl_const_Constraint_System_const_iterator_t cit)`
Invalidates the handle `cit`: this makes sure the corresponding resources will eventually be released.

Dereferencing, Incrementing and Equality Testing

- `int ppl_Constraint_System_const_iterator_dereference (ppl_const_Constraint_System_const_iterator_t cit, ppl_const_Constraint_t *pc)`
Dereference `cit` writing a const handle to the resulting constraint at address `pc`.
- `int ppl_Constraint_System_const_iterator_increment (ppl_Constraint_System_const_iterator_t cit)`
Increment `cit` so that it "points" to the next constraint.
- `int ppl_Constraint_System_const_iterator_equal_test (ppl_const_Constraint_System_const_iterator_t x, ppl_const_Constraint_System_const_iterator_t y)`
Returns a positive integer if the iterators corresponding to `x` and `y` are equal; returns 0 if they are different.

7.7.1 Detailed Description

Types and functions for iterating on constraint systems.

The types and functions for constraint systems iterators provide read-only access to the elements of a constraint system by interfacing `Constraint_System::const_iterator`.

The documentation for this interface was generated from the following file:

- `ppl_c.header.h`

7.8 `ppl_Constraint_System_tag` Interface Reference

Types and functions for constraint systems.

```
#include <ppl_c.header.h>
```

Related Functions

(Note that these are not member functions.)

Constructors, Assignment and Destructor

- int `ppl_new_Constraint_System` (`ppl_Constraint_System_t *pcs`)
Builds an empty system of constraints and writes a handle to it at address `pcs`.
- int `ppl_new_Constraint_System_zero_dim_empty` (`ppl_Constraint_System_t *pcs`)
Builds a zero-dimensional, unsatisfiable constraint system and writes a handle to it at address `pcs`.
- int `ppl_new_Constraint_System_from_Constraint` (`ppl_Constraint_System_t *pcs`, `ppl_const_Constraint_t c`)
Builds the singleton constraint system containing only a copy of constraint `c`; writes a handle for the newly created system at address `pcs`.
- int `ppl_new_Constraint_System_from_Constraint_System` (`ppl_Constraint_System_t *pcs`, `ppl_const_Constraint_System_t cs`)
Builds a constraint system that is a copy of `cs`; writes a handle for the newly created system at address `pcs`.
- int `ppl_assign_Constraint_System_from_Constraint_System` (`ppl_Constraint_System_t dst`, `ppl_const_Constraint_System_t src`)
Assigns a copy of the constraint system `src` to `dst`.
- int `ppl_delete_Constraint_System` (`ppl_const_Constraint_System_t cs`)
Invalidates the handle `cs`: this makes sure the corresponding resources will eventually be released.

Functions that Do Not Modify the Constraint System

- int `ppl_Constraint_System_space_dimension` (`ppl_const_Constraint_System_t cs`, `ppl_dimension_t *m`)
Writes to `m` the dimension of the vector space enclosing `cs`.
- int `ppl_Constraint_System_empty` (`ppl_const_Constraint_System_t cs`)
Returns a positive integer if `cs` contains no (non-trivial) constraint; returns 0 otherwise.
- int `ppl_Constraint_System_has_strict_inequalities` (`ppl_const_Constraint_System_t cs`)
Returns a positive integer if `cs` contains any (non-trivial) strict inequality; returns 0 otherwise.
- int `ppl_Constraint_System_begin` (`ppl_const_Constraint_System_t cs`, `ppl_Constraint_System_const_iterator_t cit`)
Assigns to `cit` a const iterator "pointing" to the beginning of the constraint system `cs`.
- int `ppl_Constraint_System_end` (`ppl_const_Constraint_System_t cs`, `ppl_Constraint_System_const_iterator_t cit`)
Assigns to `cit` a const iterator "pointing" past the end of the constraint system `cs`.
- int `ppl_Constraint_System_OK` (`ppl_const_Constraint_System_t cs`)
Returns a positive integer if `cs` is well formed, i.e., if it satisfies all its implementation invariants; returns 0 and perhaps makes some noise if `cs` is broken. Useful for debugging purposes.

Functions that May Modify the Constraint System

- int `ppl_Constraint_System_clear` (`ppl_Constraint_System_t cs`)
Removes all the constraints from the constraint system `cs` and sets its space dimension to 0.
- int `ppl_Constraint_System_insert_Constraint` (`ppl_Constraint_System_t cs`, `ppl_const_Constraint_t c`)
Inserts a copy of the constraint `c` into `cs`; the space dimension is increased, if necessary.

Input/Output Functions

- int `ppl_io_print_Constraint_System` (`ppl_const_Constraint_System_t x`)
Prints `x` to `stdout`.

- int `ppl_io_fprint_Constraint_System` (FILE *stream, `ppl_const_Constraint_System_t` x)
Prints x to the given output stream.
- int `ppl_io_asprint_Constraint_System` (char **strp, `ppl_const_Constraint_System_t` x)
Prints x to a malloc-allocated string, a pointer to which is returned via strp.
- int `ppl_Constraint_System_ascii_dump` (`ppl_const_Constraint_System_t` x, FILE *stream)
Dumps an ascii representation of x on stream.
- int `ppl_Constraint_System_ascii_load` (`ppl_Constraint_System_t` x, FILE *stream)
Loads an ascii representation of x from stream.

7.8.1 Detailed Description

Types and functions for constraint systems.

The types and functions for constraint systems provide an interface towards *Constraint_System*. The documentation for this interface was generated from the following file:

- `ppl_c_header.h`

7.9 ppl_Constraint_tag Interface Reference

Types and functions for constraints.

```
#include <ppl_c_header.h>
```

Related Functions

(Note that these are not member functions.)

Constructors, Assignment and Destructor

- int `ppl_new_Constraint` (`ppl_Constraint_t` *pc, `ppl_const_Linear_Expression_t` le, enum `ppl_enum_Constraint_Type` rel)
Creates the new constraint 'le rel 0' and writes a handle for it at address pc. The space dimension of the new constraint is equal to the space dimension of le.
- int `ppl_new_Constraint_zero_dim_false` (`ppl_Constraint_t` *pc)
Creates the unsatisfiable (zero-dimension space) constraint $0 = 1$ and writes a handle for it at address pc.
- int `ppl_new_Constraint_zero_dim_positivity` (`ppl_Constraint_t` *pc)
Creates the true (zero-dimension space) constraint $0 \leq 1$, also known as positivity constraint. A handle for the newly created constraint is written at address pc.
- int `ppl_new_Constraint_from_Constraint` (`ppl_Constraint_t` *pc, `ppl_const_Constraint_t` c)
Builds a constraint that is a copy of c; writes a handle for the newly created constraint at address pc.
- int `ppl_assign_Constraint_from_Constraint` (`ppl_Constraint_t` dst, `ppl_const_Constraint_t` src)
Assigns a copy of the constraint src to dst.
- int `ppl_delete_Constraint` (`ppl_const_Constraint_t` c)
Invalidates the handle c: this makes sure the corresponding resources will eventually be released.

Functions that Do Not Modify the Constraint

- int `ppl_Constraint_space_dimension` (`ppl_const_Constraint_t` c, `ppl_dimension_type` *m)
Writes to m the space dimension of c.
- int `ppl_Constraint_type` (`ppl_const_Constraint_t` c)
Returns the type of constraint c.
- int `ppl_Constraint_coefficient` (`ppl_const_Constraint_t` c, `ppl_dimension_type` var, `ppl_Coefficient_t` n)
Copies into n the coefficient of variable var in constraint c.

- int `ppl_Constraint_inhomogeneous_term` (`ppl_const_Constraint_t c`, `ppl_Coefficient_t n`)
Copies into `n` the inhomogeneous term of constraint `c`.
- int `ppl_Constraint_OK` (`ppl_const_Constraint_t c`)
Returns a positive integer if `c` is well formed, i.e., if it satisfies all its implementation invariants; returns 0 and perhaps makes some noise if `c` is broken. Useful for debugging purposes.

Input/Output Functions

- int `ppl_io_print_Constraint` (`ppl_const_Constraint_t x`)
Prints `x` to `stdout`.
- int `ppl_io_fprint_Constraint` (`FILE *stream`, `ppl_const_Constraint_t x`)
Prints `x` to the given output `stream`.
- int `ppl_io_asprint_Constraint` (`char **strp`, `ppl_const_Constraint_t x`)
Prints `x` to a malloc-allocated string, a pointer to which is returned via `strp`.
- int `ppl_Constraint_ascii_dump` (`ppl_const_Constraint_t x`, `FILE *stream`)
Dumps an ascii representation of `x` on `stream`.
- int `ppl_Constraint_ascii_load` (`ppl_Constraint_t x`, `FILE *stream`)
Loads an ascii representation of `x` from `stream`.

7.9.1 Detailed Description

Types and functions for constraints.

The types and functions for constraints provide an interface towards *Constraint*.

The documentation for this interface was generated from the following file:

- `ppl_c_header.h`

7.10 `ppl_Generator_System_const_iterator_tag` Interface Reference

Types and functions for iterating on generator systems.

```
#include <ppl_c_header.h>
```

Related Functions

(Note that these are not member functions.)

Constructors, Assignment and Destructor

- int `ppl_new_Generator_System_const_iterator` (`ppl_Generator_System_const_iterator_t *pgit`)
Builds a new 'const iterator' and writes a handle to it at address `pgit`.
- int `ppl_new_Generator_System_const_iterator_from_Generator_System_const_iterator` (`ppl_Generator_System_const_iterator_t *pgit`, `ppl_const_Generator_System_const_iterator_t git`)
Builds a const iterator that is a copy of `git`; writes a handle for the newly created const iterator at address `pgit`.
- int `ppl_assign_Generator_System_const_iterator_from_Generator_System_const_iterator` (`ppl_Generator_System_const_iterator_t dst`, `ppl_const_Generator_System_const_iterator_t src`)
Assigns a copy of the const iterator `src` to `dst`.
- int `ppl_delete_Generator_System_const_iterator` (`ppl_const_Generator_System_const_iterator_t git`)
Invalidates the handle `git`: this makes sure the corresponding resources will eventually be released.

Dereferencing, Incrementing and Equality Testing

- int `ppl_Generator_System_const_iterator_dereference` (`ppl_const_Generator_System_const_iterator_t git`, `ppl_const_Generator_t *pg`)
Dereference `git` writing a const handle to the resulting generator at address `pg`.

- `int ppl_Generator_System_const_iterator_increment (ppl_Generator_System_const_iterator_t git)`
Increment `git` so that it "points" to the next generator.
- `int ppl_Generator_System_const_iterator_equal_test (ppl_const_Generator_System_const_iterator_t x, ppl_const_Generator_System_const_iterator_t y)`
Returns a positive integer if the iterators corresponding to `x` and `y` are equal; returns 0 if they are different.

7.10.1 Detailed Description

Types and functions for iterating on generator systems.

The types and functions for generator systems iterators provide read-only access to the elements of a generator system by interfacing `Generator_System::const_iterator`.

The documentation for this interface was generated from the following file:

- `ppl_c_header.h`

7.11 `ppl_Generator_System_tag` Interface Reference

Types and functions for generator systems.

```
#include <ppl_c_header.h>
```

Related Functions

(Note that these are not member functions.)

Constructors, Assignment and Destructor

- `int ppl_new_Generator_System (ppl_Generator_System_t *pgs)`
Builds an empty system of generators and writes a handle to it at address `pgs`.
- `int ppl_new_Generator_System_from_Generator (ppl_Generator_System_t *pgs, ppl_const_Generator_t g)`
Builds the singleton generator system containing only a copy of generator `g`; writes a handle for the newly created system at address `pgs`.
- `int ppl_new_Generator_System_from_Generator_System (ppl_Generator_System_t *pgs, ppl_const_Generator_System_t gs)`
Builds a generator system that is a copy of `gs`; writes a handle for the newly created system at address `pgs`.
- `int ppl_assign_Generator_System_from_Generator_System (ppl_Generator_System_t dst, ppl_const_Generator_System_t src)`
Assigns a copy of the generator system `src` to `dst`.
- `int ppl_delete_Generator_System (ppl_const_Generator_System_t gs)`
Invalidates the handle `gs`: this makes sure the corresponding resources will eventually be released.

Functions that Do Not Modify the Generator System

- `int ppl_Generator_System_space_dimension (ppl_const_Generator_System_t gs, ppl_dimension_type *m)`
Writes to `m` the dimension of the vector space enclosing `gs`.
- `int ppl_Generator_System_empty (ppl_const_Generator_System_t gs)`
Returns a positive integer if `gs` contains no generators; returns 0 otherwise.
- `int ppl_Generator_System_begin (ppl_const_Generator_System_t gs, ppl_Generator_System_const_iterator_t git)`
Assigns to `git` a const iterator "pointing" to the beginning of the generator system `gs`.
- `int ppl_Generator_System_end (ppl_const_Generator_System_t gs, ppl_Generator_System_const_iterator_t git)`

- `int ppl_Generator_System_OK (ppl_const_Generator_System_t gs)`
Assigns to `git` a const iterator "pointing" past the end of the generator system `gs`. Returns a positive integer if `gs` is well formed, i.e., if it satisfies all its implementation invariants; returns 0 and perhaps makes some noise if `gs` is broken. Useful for debugging purposes.

Functions that May Modify the Generator System

- `int ppl_Generator_System_clear (ppl_Generator_System_t gs)`
Removes all the generators from the generator system `gs` and sets its space dimension to 0.
- `int ppl_Generator_System_insert_Generator (ppl_Generator_System_t gs, ppl_const_Generator_t g)`
Inserts a copy of the generator `g` into `gs`; the space dimension is increased, if necessary.

Input/Output Functions

- `int ppl_io_print_Generator_System (ppl_const_Generator_System_t x)`
Prints `x` to `stdout`.
- `int ppl_io_fprint_Generator_System (FILE *stream, ppl_const_Generator_System_t x)`
Prints `x` to the given output `stream`.
- `int ppl_io_asprint_Generator_System (char **strp, ppl_const_Generator_System_t x)`
Prints `x` to a malloc-allocated string, a pointer to which is returned via `strp`.
- `int ppl_Generator_System_ascii_dump (ppl_const_Generator_System_t x, FILE *stream)`
Dumps an ascii representation of `x` on `stream`.
- `int ppl_Generator_System_ascii_load (ppl_Generator_System_t x, FILE *stream)`
Loads an ascii representation of `x` from `stream`.

7.11.1 Detailed Description

Types and functions for generator systems.

The types and functions for generator systems provide an interface towards *Generator_System*. The documentation for this interface was generated from the following file:

- `ppl_c_header.h`

7.12 ppl_Generator_tag Interface Reference

Types and functions for generators.

```
#include <ppl_c_header.h>
```

Related Functions

(Note that these are not member functions.)

Constructors, Assignment and Destructor

- `int ppl_new_Generator (ppl_Generator_t *pg, ppl_const_Linear_Expression_t le, enum ppl_enum_Generator_Type t, ppl_const_Coefficient_t d)`
Creates a new generator of direction `le` and type `t`. If the generator to be created is a point or a closure point, the divisor `d` is applied to `le`. For other types of generators `d` is simply disregarded. A handle for the new generator is written at address `pg`. The space dimension of the new generator is equal to the space dimension of `le`.
- `int ppl_new_Generator_zero_dim_point (ppl_Generator_t *pg)`
Creates the point that is the origin of the zero-dimensional space \mathbb{R}^0 . Writes a handle for the new generator at address `pg`.
- `int ppl_new_Generator_zero_dim_closure_point (ppl_Generator_t *pg)`
Creates, as a closure point, the point that is the origin of the zero-dimensional space \mathbb{R}^0 . Writes a handle for the new generator at address `pg`.

- int `ppl_new_Generator_from_Generator` (`ppl_Generator_t *pg`, `ppl_const_Generator_t g`)
Builds a generator that is a copy of g ; writes a handle for the newly created generator at address pg .
- int `ppl_assign_Generator_from_Generator` (`ppl_Generator_t dst`, `ppl_const_Generator_t src`)
Assigns a copy of the generator src to dst .
- int `ppl_delete_Generator` (`ppl_const_Generator_t g`)
Invalidates the handle g : this makes sure the corresponding resources will eventually be released.

Functions that Do Not Modify the Generator

- int `ppl_Generator_space_dimension` (`ppl_const_Generator_t g`, `ppl_dimension_type *m`)
Writes to m the space dimension of g .
- int `ppl_Generator_type` (`ppl_const_Generator_t g`)
Returns the type of generator g .
- int `ppl_Generator_coefficient` (`ppl_const_Generator_t g`, `ppl_dimension_type var`, `ppl_Coefficient_t n`)
Copies into n the coefficient of variable var in generator g .
- int `ppl_Generator_divisor` (`ppl_const_Generator_t g`, `ppl_Coefficient_t n`)
If g is a point or a closure point assigns its divisor to n .
- int `ppl_Generator_OK` (`ppl_const_Generator_t g`)
Returns a positive integer if g is well formed, i.e., if it satisfies all its implementation invariants; returns 0 and perhaps makes some noise if g is broken. Useful for debugging purposes.

Input/Output Functions

- int `ppl_io_print_Generator` (`ppl_const_Generator_t x`)
Prints x to `stdout`.
- int `ppl_io_fprint_Generator` (`FILE *stream`, `ppl_const_Generator_t x`)
Prints x to the given output `stream`.
- int `ppl_io_asprint_Generator` (`char **strp`, `ppl_const_Generator_t x`)
Prints x to a malloc-allocated string, a pointer to which is returned via `strp`.
- int `ppl_Generator_ascii_dump` (`ppl_const_Generator_t x`, `FILE *stream`)
Dumps an ascii representation of x on `stream`.
- int `ppl_Generator_ascii_load` (`ppl_Generator_t x`, `FILE *stream`)
Loads an ascii representation of x from `stream`.

7.12.1 Detailed Description

Types and functions for generators.

The types and functions for generators provide an interface towards *Generator*.

The documentation for this interface was generated from the following file:

- `ppl_c_header.h`

7.13 `ppl_Grid_Generator_System_const_iterator_tag` Interface Reference

Types and functions for iterating on grid generator systems.

```
#include <ppl_c_header.h>
```

Related Functions

(Note that these are not member functions.)

Constructors, Assignment and Destructor

- `int ppl_new_Grid_Generator_System_const_iterator (ppl_Grid_Generator_System_const_iterator_t *pgit)`
Builds a new 'const iterator' and writes a handle to it at address `pgit`.
- `int ppl_new_Grid_Generator_System_const_iterator_from_Grid_Generator_System_const_iterator (ppl_Grid_Generator_System_const_iterator_t *pgit, ppl_const_Grid_Generator_System_const_iterator_t git)`
Builds a const iterator that is a copy of `git`; writes a handle for the newly created const iterator at address `pgit`.
- `int ppl_assign_Grid_Generator_System_const_iterator_from_Grid_Generator_System_const_iterator (ppl_Grid_Generator_System_const_iterator_t dst, ppl_const_Grid_Generator_System_const_iterator_t src)`
Assigns a copy of the const iterator `src` to `dst`.
- `int ppl_delete_Grid_Generator_System_const_iterator (ppl_const_Grid_Generator_System_const_iterator_t git)`
Invalidates the handle `git`: this makes sure the corresponding resources will eventually be released.

Dereferencing, Incrementing and Equality Testing

- `int ppl_Grid_Generator_System_const_iterator_dereference (ppl_const_Grid_Generator_System_const_iterator_t git, ppl_const_Grid_Generator_t *pg)`
Dereference `git` writing a const handle to the resulting grid generator at address `pg`.
- `int ppl_Grid_Generator_System_const_iterator_increment (ppl_Grid_Generator_System_const_iterator_t git)`
Increment `git` so that it "points" to the next grid generator.
- `int ppl_Grid_Generator_System_const_iterator_equal_test (ppl_const_Grid_Generator_System_const_iterator_t x, ppl_const_Grid_Generator_System_const_iterator_t y)`
Returns a positive integer if the iterators corresponding to `x` and `y` are equal; returns 0 if they are different.

7.13.1 Detailed Description

Types and functions for iterating on grid generator systems.

The types and functions for grid generator systems iterators provide read-only access to the elements of a grid generator system by interfacing `Grid_Generator_System::const_iterator`.

The documentation for this interface was generated from the following file:

- `ppl_c.header.h`

7.14 `ppl_Grid_Generator_System_tag` Interface Reference

Types and functions for grid generator systems.

```
#include <ppl_c.header.h>
```

Related Functions

(Note that these are not member functions.)

Constructors, Assignment and Destructor

- `int ppl_new_Grid_Generator_System (ppl_Grid_Generator_System_t *pgs)`

- Builds an empty system of grid generators and writes a handle to it at address `pgs`.*

• `int ppl_new_Grid_Generator_System_from_Grid_Generator (ppl_Grid_Generator_System_t *pgs, ppl_const_Grid_Generator_t g)`

Builds the singleton grid generator system containing only a copy of generator `g`; writes a handle for the newly created system at address `pgs`.
- `int ppl_new_Grid_Generator_System_from_Grid_Generator_System (ppl_Grid_Generator_System_t *pgs, ppl_const_Grid_Generator_System_t gs)`

Builds a grid generator system that is a copy of `gs`; writes a handle for the newly created system at address `pgs`.
- `int ppl_assign_Grid_Generator_System_from_Grid_Generator_System (ppl_Grid_Generator_System_t dst, ppl_const_Grid_Generator_System_t src)`

Assigns a copy of the grid generator system `src` to `dst`.
- `int ppl_delete_Grid_Generator_System (ppl_const_Grid_Generator_System_t gs)`

Invalidates the handle `gs`: this makes sure the corresponding resources will eventually be released.

Functions that Do Not Modify the Grid Generator System

- `int ppl_Grid_Generator_System_space_dimension (ppl_const_Grid_Generator_System_t gs, ppl_dimension_type *m)`

Writes to `m` the dimension of the vector space enclosing `gs`.
- `int ppl_Grid_Generator_System_empty (ppl_const_Grid_Generator_System_t gs)`

Returns a positive integer if `gs` contains no generator; returns 0 otherwise.
- `int ppl_Grid_Generator_System_begin (ppl_const_Grid_Generator_System_t gs, ppl_Grid_Generator_System_const_iterator_t git)`

Assigns to `git` a const iterator "pointing" to the beginning of the grid generator system `gs`.
- `int ppl_Grid_Generator_System_end (ppl_const_Grid_Generator_System_t gs, ppl_Grid_Generator_System_const_iterator_t git)`

Assigns to `git` a const iterator "pointing" past the end of the grid generator system `gs`.
- `int ppl_Grid_Generator_System_OK (ppl_const_Grid_Generator_System_t gs)`

Returns a positive integer if `gs` is well formed, i.e., if it satisfies all its implementation invariants; returns 0 and perhaps makes some noise if `gs` is broken. Useful for debugging purposes.

Functions that May Modify the Grid Generator System

- `int ppl_Grid_Generator_System_clear (ppl_Grid_Generator_System_t gs)`

Removes all the generators from the grid generator system `gs` and sets its space dimension to 0.
- `int ppl_Grid_Generator_System_insert_Grid_Generator (ppl_Grid_Generator_System_t gs, ppl_const_Grid_Generator_t g)`

Inserts a copy of the grid generator `g` into `gs`; the space dimension is increased, if necessary.

Input/Output Functions

- `int ppl_io_print_Grid_Generator_System (ppl_const_Grid_Generator_System_t x)`

Prints `x` to `stdout`.
- `int ppl_io_fprint_Grid_Generator_System (FILE *stream, ppl_const_Grid_Generator_System_t x)`

Prints `x` to the given output `stream`.
- `int ppl_io_asprint_Grid_Generator_System (char **strp, ppl_const_Grid_Generator_System_t x)`

Prints `x` to a malloc-allocated string, a pointer to which is returned via `strp`.
- `int ppl_Grid_Generator_System_ascii_dump (ppl_const_Grid_Generator_System_t x, FILE *stream)`

Dumps an ascii representation of `x` on `stream`.
- `int ppl_Grid_Generator_System_ascii_load (ppl_Grid_Generator_System_t x, FILE *stream)`

Loads an ascii representation of `x` from `stream`.

7.14.1 Detailed Description

Types and functions for grid generator systems.

The types and functions for grid generator systems provide an interface towards *Grid_Generator_System*.

The documentation for this interface was generated from the following file:

- `ppl_c_header.h`

7.15 `ppl_Grid_Generator_tag` Interface Reference

Types and functions for grid generators.

```
#include <ppl_c_header.h>
```

Related Functions

(Note that these are not member functions.)

Constructors, Assignment and Destructor

- `int ppl_new_Grid_Generator (ppl_Grid_Generator_t *pg, ppl_const_Linear_Expression_t le, enum ppl_enum_Grid_Generator_Type t, ppl_const_Coefficient_t d)`
Creates a new grid generator of direction `le` and type `t`. If the grid generator to be created is a point or a parameter, the divisor `d` is applied to `le`. If it is a line, `d` is simply disregarded. A handle for the new grid generator is written at address `pg`. The space dimension of the new grid generator is equal to the space dimension of `le`.
- `int ppl_new_Grid_Generator_zero_dim_point (ppl_Grid_Generator_t *pg)`
Creates the point that is the origin of the zero-dimensional space \mathbb{R}^0 . Writes a handle for the new grid generator at address `pg`.
- `int ppl_new_Grid_Generator_from_Grid_Generator (ppl_Grid_Generator_t *pg, ppl_const_Grid_Generator_t g)`
Builds a grid generator that is a copy of `g`; writes a handle for the newly created grid generator at address `pg`.
- `int ppl_assign_Grid_Generator_from_Grid_Generator (ppl_Grid_Generator_t dst, ppl_const_Grid_Generator_t src)`
Assigns a copy of the grid generator `src` to `dst`.
- `int ppl_delete_Grid_Generator (ppl_const_Grid_Generator_t g)`
Invalidates the handle `g`: this makes sure the corresponding resources will eventually be released.

Functions that Do Not Modify the Grid Generator

- `int ppl_Grid_Generator_space_dimension (ppl_const_Grid_Generator_t g, ppl_dimension_type *m)`
Writes to `m` the space dimension of `g`.
- `int ppl_Grid_Generator_type (ppl_const_Grid_Generator_t g)`
Returns the type of grid generator `g`.
- `int ppl_Grid_Generator_coefficient (ppl_const_Grid_Generator_t g, ppl_dimension_type var, ppl_Coefficient_t n)`
Copies into `n` the coefficient of variable `var` in grid generator `g`.
- `int ppl_Grid_Generator_divisor (ppl_const_Grid_Generator_t g, ppl_Coefficient_t n)`
If `g` is a point or a parameter assigns its divisor to `n`.
- `int ppl_Grid_Generator_OK (ppl_const_Grid_Generator_t g)`
Returns a positive integer if `g` is well formed, i.e., if it satisfies all its implementation invariants; returns 0 and perhaps makes some noise if `g` is broken. Useful for debugging purposes.

Input/Output Functions

- int `ppl_io_print_Grid_Generator` (`ppl_const_Grid_Generator_t x`)
Prints x to `stdout`.
- int `ppl_io_fprint_Grid_Generator` (`FILE *stream`, `ppl_const_Grid_Generator_t x`)
Prints x to the given output `stream`.
- int `ppl_io_asprint_Grid_Generator` (`char **strp`, `ppl_const_Grid_Generator_t x`)
Prints x to a malloc-allocated string, a pointer to which is returned via `strp`.
- int `ppl_Grid_Generator_ascii_dump` (`ppl_const_Grid_Generator_t x`, `FILE *stream`)
Dumps an ascii representation of x on `stream`.
- int `ppl_Grid_Generator_ascii_load` (`ppl_Grid_Generator_t x`, `FILE *stream`)
Loads an ascii representation of x from `stream`.

7.15.1 Detailed Description

Types and functions for grid generators.

The types and functions for grid generators provide an interface towards *Grid_Generator*.
The documentation for this interface was generated from the following file:

- `ppl_c_header.h`

7.16 `ppl_Linear_Expression_tag` Interface Reference

Types and functions for linear expressions.

```
#include <ppl_c_header.h>
```

Related Functions

(Note that these are not member functions.)

Constructors, Assignment and Destructor

- int `ppl_new_Linear_Expression` (`ppl_Linear_Expression_t *ple`)
Creates a new linear expression corresponding to the constant 0 in a zero-dimensional space; writes a handle for the new linear expression at address `ple`.
- int `ppl_new_Linear_Expression_with_dimension` (`ppl_Linear_Expression_t *ple`, `ppl_dimension_t d`)
Creates a new linear expression corresponding to the constant 0 in a d -dimensional space; writes a handle for the new linear expression at address `ple`.
- int `ppl_new_Linear_Expression_from_Linear_Expression` (`ppl_Linear_Expression_t *ple`, `ppl_const_Linear_Expression_t le`)
Builds a linear expression that is a copy of `le`; writes a handle for the newly created linear expression at address `ple`.
- int `ppl_new_Linear_Expression_from_Constraint` (`ppl_Linear_Expression_t *ple`, `ppl_const_Constraint_t c`)
Builds a linear expression corresponding to constraint `c`; writes a handle for the newly created linear expression at address `ple`.
- int `ppl_new_Linear_Expression_from_Generator` (`ppl_Linear_Expression_t *ple`, `ppl_const_Generator_t g`)
Builds a linear expression corresponding to generator `g`; writes a handle for the newly created linear expression at address `ple`.
- int `ppl_new_Linear_Expression_from_Congruence` (`ppl_Linear_Expression_t *ple`, `ppl_const_Congruence_t c`)
Builds a linear expression corresponding to congruence `c`; writes a handle for the newly created linear expression at address `ple`.
- int `ppl_new_Linear_Expression_from_Grid_Generator` (`ppl_Linear_Expression_t *ple`, `ppl_const_Grid_Generator_t g`)

Builds a linear expression corresponding to grid generator g ; writes a handle for the newly created linear expression at address p_{le} .

- `int ppl_assign_Linear_Expression_from_Linear_Expression (ppl_Linear_Expression_t dst, ppl_const_Linear_Expression_t src)`
Assigns a copy of the linear expression src to dst .
- `int ppl_delete_Linear_Expression (ppl_const_Linear_Expression_t le)`
Invalidates the handle le : this makes sure the corresponding resources will eventually be released.

Functions that Do Not Modify the Linear Expression

- `int ppl_Linear_Expression_space_dimension (ppl_const_Linear_Expression_t le, ppl_dimension_type *m)`
Writes to m the space dimension of le .
- `int ppl_Linear_Expression_coefficient (ppl_const_Linear_Expression_t le, ppl_dimension_type var, ppl_Coefficient_t n)`
Copies into n the coefficient of variable var in the linear expression le .
- `int ppl_Linear_Expression_inhomogeneous_term (ppl_const_Linear_Expression_t le, ppl_Coefficient_t n)`
Copies into n the inhomogeneous term of linear expression le .
- `int ppl_Linear_Expression_OK (ppl_const_Linear_Expression_t le)`
Returns a positive integer if le is well formed, i.e., if it satisfies all its implementation invariants; returns 0 and perhaps makes some noise if le is broken. Useful for debugging purposes.
- `int ppl_Linear_Expression_is_zero (ppl_const_Linear_Expression_t le)`
*Returns `true` if and only if $*this$ is 0.*
- `int ppl_Linear_Expression_all_homogeneous_terms_are_zero (ppl_const_Linear_Expression_t le)`
*Returns `true` if and only if all the homogeneous terms of $*this$ are 0.*

Functions that May Modify the Linear Expression

- `int ppl_Linear_Expression_add_to_coefficient (ppl_Linear_Expression_t le, ppl_dimension_type var, ppl_const_Coefficient_t n)`
Adds n to the coefficient of variable var in the linear expression le . The space dimension is set to be the maximum between $var + 1$ and the old space dimension.
- `int ppl_Linear_Expression_add_to_inhomogeneous (ppl_Linear_Expression_t le, ppl_const_Coefficient_t n)`
Adds n to the inhomogeneous term of the linear expression le .
- `int ppl_add_Linear_Expression_to_Linear_Expression (ppl_Linear_Expression_t dst, ppl_const_Linear_Expression_t src)`
Adds the linear expression src to dst .
- `int ppl_subtract_Linear_Expression_from_Linear_Expression (ppl_Linear_Expression_t dst, ppl_const_Linear_Expression_t src)`
Subtracts the linear expression src from dst .
- `int ppl_multiply_Linear_Expression_by_Coefficient (ppl_Linear_Expression_t le, ppl_const_Coefficient_t n)`
Multiply the linear expression dst by n .

Input/Output Functions

- `int ppl_io_print_Linear_Expression (ppl_const_Linear_Expression_t x)`
Prints x to `stdout`.
- `int ppl_io_fprint_Linear_Expression (FILE *stream, ppl_const_Linear_Expression_t x)`
Prints x to the given output `stream`.
- `int ppl_io_asprint_Linear_Expression (char **strp, ppl_const_Linear_Expression_t x)`
Prints x to a malloc-allocated string, a pointer to which is returned via `strp`.
- `int ppl_Linear_Expression_ascii_dump (ppl_const_Linear_Expression_t x, FILE *stream)`
Dumps an ascii representation of x on `stream`.
- `int ppl_Linear_Expression_ascii_load (ppl_Linear_Expression_t x, FILE *stream)`
Loads an ascii representation of x from `stream`.

7.16.1 Detailed Description

Types and functions for linear expressions.

The types and functions for linear expression provide an interface towards *Linear_Expression*.

The documentation for this interface was generated from the following file:

- `ppl_c_header.h`

7.17 `ppl_MIP_Problem_tag` Interface Reference

Types and functions for MIP problems.

```
#include <ppl_c_header.h>
```

Related Functions

(Note that these are not member functions.)

Symbolic Constants

- `int PPL_OPTIMIZATION_MODE_MAXIMIZATION`
Code of the "maximization" optimization mode.
- `int PPL_OPTIMIZATION_MODE_MINIMIZATION`
Code of the "minimization" optimization mode.
- `int PPL_MIP_PROBLEM_STATUS_UNFEASIBLE`
Code of the "unfeasible MIP problem" status.
- `int PPL_MIP_PROBLEM_STATUS_UNBOUNDED`
Code of the "unbounded MIP problem" status.
- `int PPL_MIP_PROBLEM_STATUS_OPTIMIZED`
Code of the "optimized MIP problem" status.
- `int PPL_MIP_PROBLEM_CONTROL_PARAMETER_NAME_PRICING`
Code for the MIP problem's "pricing" control parameter name.
- `int PPL_MIP_PROBLEM_CONTROL_PARAMETER_PRICING_TEXTBOOK`
Code of MIP problem's "textbook" pricing method.
- `int PPL_MIP_PROBLEM_CONTROL_PARAMETER_PRICING_STEEPEST_EDGE_EXACT`
Code of MIP problem's "exact steepest-edge" pricing method.
- `int PPL_MIP_PROBLEM_CONTROL_PARAMETER_PRICING_STEEPEST_EDGE_FLOAT`
Code of MIP problem's "float steepest-edge" pricing method.

Constructors, Assignment and Destructor

- `int ppl_new_MIP_Problem_from_space_dimension (ppl_MIP_Problem_t *pmip, ppl_dimension_type d)`
Builds a trivial MIP problem of dimension `d` and writes a handle to it at address `pmip`.
- `int ppl_new_MIP_Problem (ppl_MIP_Problem_t *pmip, ppl_dimension_type d, ppl_const_Constraint_System_t cs, ppl_const_Linear_Expression_t le, int m)`
Builds a MIP problem of space dimension `d` having feasible region `cs`, objective function `le` and optimization mode `m`; writes a handle to it at address `pmip`.
- `int ppl_new_MIP_Problem_from_MIP_Problem (ppl_MIP_Problem_t *pmip, ppl_const_MIP_Problem_t mip)`
Builds a MIP problem that is a copy of `mip`; writes a handle for the newly created system at address `pmip`.
- `int ppl_assign_MIP_Problem_from_MIP_Problem (ppl_MIP_Problem_t dst, ppl_const_MIP_Problem_t src)`
Assigns a copy of the MIP problem `src` to `dst`.

- int `ppl_delete_MIP_Problem` (`ppl_const_MIP_Problem_t mip`)
Invalidates the handle `mip`: this makes sure the corresponding resources will eventually be released.

Functions that Do Not Modify the MIP_Problem

- int `ppl_MIP_Problem_space_dimension` (`ppl_const_MIP_Problem_t mip`, `ppl_dimension_type *m`)
Writes to `m` the dimension of the vector space enclosing `mip`.
- int `ppl_MIP_Problem_number_of_integer_space_dimensions` (`ppl_const_MIP_Problem_t mip`, `ppl_dimension_type *m`)
Writes to `m` the number of integer space dimensions of `mip`.
- int `ppl_MIP_Problem_integer_space_dimensions` (`ppl_const_MIP_Problem_t mip`, `ppl_dimension_type ds[]`)
Writes in the first positions of the array `ds` all the integer space dimensions of problem `mip`. If the array is not big enough to hold all of the integer space dimensions, the behavior is undefined.
- int `ppl_MIP_Problem_number_of_constraints` (`ppl_const_MIP_Problem_t mip`, `ppl_dimension_type *m`)
Writes to `m` the number of constraints defining the feasible region of `mip`.
- int `ppl_MIP_Problem_constraint_at_index` (`ppl_const_MIP_Problem_t mip`, `ppl_dimension_type i`, `ppl_const_Constraint_t *pc`)
Writes at address `pc` a const handle to the `i`-th constraint defining the feasible region of the MIP problem `mip`.
- int `ppl_MIP_Problem_objective_function` (`ppl_const_MIP_Problem_t mip`, `ppl_const_Linear_Expression_t *ple`)
Writes a const handle to the linear expression defining the objective function of the MIP problem `mip` at address `ple`.
- int `ppl_MIP_Problem_optimization_mode` (`ppl_const_MIP_Problem_t mip`)
Returns the optimization mode of the MIP problem `mip`.
- int `ppl_MIP_Problem_OK` (`ppl_const_MIP_Problem_t mip`)
Returns a positive integer if `mip` is well formed, i.e., if it satisfies all its implementation invariants; returns 0 and perhaps makes some noise if `mip` is broken. Useful for debugging purposes.

Functions that May Modify the MIP_Problem

- int `ppl_MIP_Problem_clear` (`ppl_MIP_Problem_t mip`)
Resets the MIP problem to be a trivial problem of space dimension 0.
- int `ppl_MIP_Problem_add_space_dimensions_and_embed` (`ppl_MIP_Problem_t mip`, `ppl_dimension_type d`)
Adds `d` new dimensions to the space enclosing the MIP problem `mip` and to `mip` itself.
- int `ppl_MIP_Problem_add_to_integer_space_dimensions` (`ppl_MIP_Problem_t mip`, `ppl_dimension_type ds[]`, `size_t n`)
Sets the space dimensions that are specified in first `n` positions of the array `ds` to be integer dimensions of problem `mip`. The presence of duplicates in `ds` is a waste but an innocuous one.
- int `ppl_MIP_Problem_add_constraint` (`ppl_MIP_Problem_t mip`, `ppl_const_Constraint_t c`)
Modifies the feasible region of the MIP problem `mip` by adding a copy of the constraint `c`.
- int `ppl_MIP_Problem_add_constraints` (`ppl_MIP_Problem_t mip`, `ppl_const_Constraint_System_t cs`)
Modifies the feasible region of the MIP problem `mip` by adding a copy of the constraints in `cs`.
- int `ppl_MIP_Problem_set_objective_function` (`ppl_MIP_Problem_t mip`, `ppl_const_Linear_Expression_t le`)
Sets the objective function of the MIP problem `mip` to a copy of `le`.
- int `ppl_MIP_Problem_set_optimization_mode` (`ppl_MIP_Problem_t mip`, `int mode`)
Sets the optimization mode of the MIP problem `mip` to `mode`.

Computing the Solution of the MIP_Problem

- int `ppl_MIP_Problem_is_satisfiable` (`ppl_const_MIP_Problem_t mip`)
Returns a positive integer if `mip` is satisfiable; returns 0 otherwise.
- int `ppl_MIP_Problem_solve` (`ppl_const_MIP_Problem_t mip`)
Solves the MIP problem `mip`, returning an exit status.
- int `ppl_MIP_Problem_evaluate_objective_function` (`ppl_const_MIP_Problem_t mip`, `ppl_const_Generator_t g`, `ppl_Coefficient_t num`, `ppl_Coefficient_t den`)
Evaluates the objective function of `mip` on point `g`.
- int `ppl_MIP_Problem_feasible_point` (`ppl_const_MIP_Problem_t mip`, `ppl_const_Generator_t *pg`)
Writes a const handle to a feasible point for the MIP problem `mip` at address `pg`.
- int `ppl_MIP_Problem_optimizing_point` (`ppl_const_MIP_Problem_t mip`, `ppl_const_Generator_t *pg`)
Writes a const handle to an optimizing point for the MIP problem `mip` at address `pg`.
- int `ppl_MIP_Problem_optimal_value` (`ppl_const_MIP_Problem_t mip`, `ppl_Coefficient_t num`, `ppl_Coefficient_t den`)
Returns the optimal value for `mip`.

Querying/Setting Control Parameters

- int `ppl_MIP_Problem_get_control_parameter` (`ppl_const_MIP_Problem_t mip`, int name)
Returns the value of control parameter name in problem `mip`.
- int `ppl_MIP_Problem_set_control_parameter` (`ppl_MIP_Problem_t mip`, int value)
Sets control parameter value in problem `mip`.
- int `ppl_MIP_Problem_total_memory_in_bytes` (`ppl_const_MIP_Problem_t mip`, `size_t *sz`)
*Writes into `*sz` the size in bytes of the memory occupied by `mip`.*
- int `ppl_MIP_Problem_external_memory_in_bytes` (`ppl_const_MIP_Problem_t mip`, `size_t *sz`)
*Writes into `*sz` the size in bytes of the memory managed by `mip`.*

Input/Output Functions

- int `ppl_io_print_MIP_Problem` (`ppl_const_MIP_Problem_t x`)
Prints `x` to `stdout`.
- int `ppl_io_fprint_MIP_Problem` (FILE *stream, `ppl_const_MIP_Problem_t x`)
Prints `x` to the given output stream.
- int `ppl_io_asprint_MIP_Problem` (char **strp, `ppl_const_MIP_Problem_t x`)
Prints `x` to a malloc-allocated string, a pointer to which is returned via `strp`.
- int `ppl_MIP_Problem_ascii_dump` (`ppl_const_MIP_Problem_t x`, FILE *stream)
Dumps an ascii representation of `x` on stream.
- int `ppl_MIP_Problem_ascii_load` (`ppl_MIP_Problem_t x`, FILE *stream)
Loads an ascii representation of `x` from stream.

7.17.1 Detailed Description

Types and functions for MIP problems.

The types and functions for MIP problems provide an interface towards *MIP_Problem*.

7.17.2 Friends And Related Function Documentation

int `ppl_MIP_Problem_solve` (`ppl_const_MIP_Problem_t mip`) [**related**] Solves the MIP problem `mip`, returning an exit status.

Returns

`PPL_MIP_PROBLEM_STATUS_UNFEASIBLE` if the MIP problem is not satisfiable; `PPL_MIP_PROBLEM_STATUS_UNBOUNDED` if the MIP problem is satisfiable but there is no finite bound to the value of the objective function; `PPL_MIP_PROBLEM_STATUS_OPTIMIZED` if the MIP problem admits an optimal solution.

int ppl_MIP_Problem_evaluate_objective_function (ppl_const_MIP_Problem_t mip, ppl_const_Generator_t g, ppl_Coefficient_t num, ppl_Coefficient_t den) [related] Evaluates the objective function of mip on point g.

Parameters

<i>mip</i>	The MIP problem defining the objective function;
<i>g</i>	The generator on which the objective function will be evaluated;
<i>num</i>	Will be assigned the numerator of the objective function value;
<i>den</i>	Will be assigned the denominator of the objective function value;

int ppl_MIP_Problem_optimal_value (ppl_const_MIP_Problem_t mip, ppl_Coefficient_t num, ppl_Coefficient_t den) [**related**] Returns the optimal value for *mip*.

Parameters

<i>mip</i>	The MIP problem;
<i>num</i>	Will be assigned the numerator of the optimal value;
<i>den</i>	Will be assigned the denominator of the optimal value.

The documentation for this interface was generated from the following file:

- `ppl_c_header.h`

7.18 ppl_PIP_Decision_Node_tag Interface Reference

Types and functions for PIP decision nodes.

```
#include <ppl_c_header.h>
```

Related Functions

(Note that these are not member functions.)

- **int ppl_PIP_Decision_Node_get_child_node (ppl_const_PIP_Decision_Node_t pip_dec, int b, ppl_const_PIP_Tree_Node_t *pip_tree)**

Writes to pip_tree a const pointer to either the true branch (if b is not zero) or the false branch (if b is zero) of pip_dec.

Input/Output Functions

- **int ppl_io_print_PIP_Decision_Node (ppl_const_PIP_Decision_Node_t x)**
Prints x to stdout.
- **int ppl_io_fprint_PIP_Decision_Node (FILE *stream, ppl_const_PIP_Decision_Node_t x)**
Prints x to the given output stream.
- **int ppl_io_asprint_PIP_Decision_Node (char **strp, ppl_const_PIP_Decision_Node_t x)**
Prints x to a malloc-allocated string, a pointer to which is returned via strp.
- **int ppl_PIP_Decision_Node_ascii_dump (ppl_const_PIP_Decision_Node_t x, FILE *stream)**
Dumps an ascii representation of x on stream.
- **int ppl_PIP_Decision_Node_ascii_load (ppl_PIP_Decision_Node_t x, FILE *stream)**
Loads an ascii representation of x from stream.

7.18.1 Detailed Description

Types and functions for PIP decision nodes.

The types and functions for decision nodes provide an interface towards *PIP_Decision_Node*.

The documentation for this interface was generated from the following file:

- `ppl_c_header.h`

7.19 ppl_PIP_Problem_tag Interface Reference

Types and functions for PIP problems.

```
#include <ppl_c_header.h>
```

Related Functions

(Note that these are not member functions.)

Symbolic Constants

- int `PPL_PIP_PROBLEM_STATUS_UNFEASIBLE`
Code of the "unfeasible PIP problem" status.
- int `PPL_PIP_PROBLEM_STATUS_OPTIMIZED`
Code of the "optimized PIP problem" status.
- int `PPL_PIP_PROBLEM_CONTROL_PARAMETER_NAME_CUTTING_STRATEGY`
Code for the PIP problem's "cutting strategy" control parameter name.
- int `PPL_PIP_PROBLEM_CONTROL_PARAMETER_NAME_PIVOT_ROW_STRATEGY`
Code for the PIP problem's "pivot row strategy" control parameter name.
- int `PPL_PIP_PROBLEM_CONTROL_PARAMETER_CUTTING_STRATEGY_FIRST`
Code of PIP problem's "first" cutting strategy.
- int `PPL_PIP_PROBLEM_CONTROL_PARAMETER_CUTTING_STRATEGY_DEEPEST`
Code of PIP problem's "deepest" cutting strategy.
- int `PPL_PIP_PROBLEM_CONTROL_PARAMETER_CUTTING_STRATEGY_ALL`
Code of PIP problem's "all" cutting strategy.
- int `PPL_PIP_PROBLEM_CONTROL_PARAMETER_PIVOT_ROW_STRATEGY_FIRST`
Code of PIP problem's "first" pivot row strategy.
- int `PPL_PIP_PROBLEM_CONTROL_PARAMETER_PIVOT_ROW_STRATEGY_MAX_COLUMN`
Code of PIP problem's "max column" pivot row strategy.

Constructors, Assignment and Destructor

- int `ppl_new_PIP_Problem_from_space_dimension` (`ppl_PIP_Problem_t *ppip`, `ppl_dimension_type d`)
Builds a trivial PIP problem of dimension `d` and writes a handle to it at address `ppip`.
- int `ppl_new_PIP_Problem_from_PIP_Problem` (`ppl_PIP_Problem_t *ppip`, `ppl_const_PIP_Problem_t pip`)
Builds a PIP problem that is a copy of `pip`; writes a handle for the newly created problem at address `ppip`.
- int `ppl_assign_PIP_Problem_from_PIP_Problem` (`ppl_PIP_Problem_t dst`, `ppl_const_PIP_Problem_t src`)
Assigns a copy of the PIP problem `src` to `dst`.
- int `ppl_new_PIP_Problem_from_constraints` (`ppl_PIP_Problem_t *ppip`, `ppl_dimension_type d`, `ppl_Constraint_System_const_iterator_t first`, `ppl_Constraint_System_const_iterator_t last`, `size_t n`, `ppl_dimension_type ds[]`)
Builds a PIP problem having space dimension `d` from the sequence of constraints in the range `[first, last)`; the `n` dimensions whose indices occur in `ds` are interpreted as parameters.
- int `ppl_delete_PIP_Problem` (`ppl_const_PIP_Problem_t pip`)
Invalidates the handle `pip`: this makes sure the corresponding resources will eventually be released.

Functions that Do Not Modify the PIP_Problem

- int `ppl_PIP_Problem_space_dimension` (`ppl_const_PIP_Problem_t pip`, `ppl_dimension_type *m`)

- Writes to m the dimension of the vector space enclosing pip .
- int `ppl_PIP_Problem_number_of_parameter_space_dimensions` (`ppl_const_PIP_Problem_t pip`, `ppl_dimension_type *m`)

Writes to m the number of parameter space dimensions of pip .
- int `ppl_PIP_Problem_parameter_space_dimensions` (`ppl_const_PIP_Problem_t pip`, `ppl_dimension_type ds[]`)

Writes in the first positions of the array ds all the parameter space dimensions of problem pip . If the array is not big enough to hold all of the parameter space dimensions, the behavior is undefined.
- int `ppl_PIP_Problem_get_big_parameter_dimension` (`ppl_const_PIP_Problem_t pip`, `ppl_dimension_type *pd`)

Writes into $*pd$ the big parameter dimension of PIP problem pip .
- int `ppl_PIP_Problem_number_of_constraints` (`ppl_const_PIP_Problem_t pip`, `ppl_dimension_type *m`)

Writes to m the number of constraints defining the feasible region of pip .
- int `ppl_PIP_Problem_constraint_at_index` (`ppl_const_PIP_Problem_t pip`, `ppl_dimension_type i`, `ppl_const_Constraint_t *pc`)

Writes at address pc a const handle to the i -th constraint defining the feasible region of the PIP problem pip .
- int `ppl_PIP_Problem_total_memory_in_bytes` (`ppl_const_PIP_Problem_t pip`, `size_t *sz`)

Writes into $*sz$ the size in bytes of the memory occupied by pip .
- int `ppl_PIP_Problem_external_memory_in_bytes` (`ppl_const_PIP_Problem_t pip`, `size_t *sz`)

Writes into $*sz$ the size in bytes of the memory managed by pip .
- int `ppl_PIP_Problem_OK` (`ppl_const_PIP_Problem_t pip`)

Returns a positive integer if pip is well formed, i.e., if it satisfies all its implementation invariants; returns 0 and perhaps makes some noise if pip is broken. Useful for debugging purposes.

Functions that May Modify the PIP Problem

- int `ppl_PIP_Problem_clear` (`ppl_PIP_Problem_t pip`)

Resets the PIP problem to be a trivial problem of space dimension 0.
- int `ppl_PIP_Problem_add_space_dimensions_and_embed` (`ppl_PIP_Problem_t pip`, `ppl_dimension_type pip_vars`, `ppl_dimension_type pip_params`)

Adds $pip_vars + pip_params$ new space dimensions and embeds the PIP problem pip in the new vector space.
- int `ppl_PIP_Problem_add_to_parameter_space_dimensions` (`ppl_PIP_Problem_t pip`, `ppl_dimension_type ds[]`, `size_t n`)

Sets the space dimensions that are specified in first n positions of the array ds to be parameter dimensions of problem pip . The presence of duplicates in ds is a waste but an innocuous one.
- int `ppl_PIP_Problem_set_big_parameter_dimension` (`ppl_PIP_Problem_t pip`, `ppl_dimension_type d`)

Sets the big parameter dimension of PIP problem pip to d .
- int `ppl_PIP_Problem_add_constraint` (`ppl_PIP_Problem_t pip`, `ppl_const_Constraint_t c`)

Modifies the feasible region of the PIP problem pip by adding a copy of the constraint c .
- int `ppl_PIP_Problem_add_constraints` (`ppl_PIP_Problem_t pip`, `ppl_const_Constraint_System_t cs`)

Modifies the feasible region of the PIP problem pip by adding a copy of the constraints in cs .

Computing and Printing the Solution of the PIP Problem

- int `ppl_PIP_Problem_is_satisfiable` (`ppl_const_PIP_Problem_t pip`)

Returns a positive integer if pip is satisfiable and an optimal solution can be found; returns 0 otherwise.
- int `ppl_PIP_Problem_solve` (`ppl_const_PIP_Problem_t pip`)

Solves the PIP problem pip , returning an exit status.
- int `ppl_PIP_Problem_solution` (`ppl_const_PIP_Problem_t pip`, `ppl_const_PIP_Tree_Node_t *pip_tree`)

Writes to `pip_tree` a solution for `pip`, if it exists.

- `int ppl_PIP_Problem_optimizing_solution (ppl_const_PIP_Problem_t pip, ppl_const_PIP_Tree_Node_t *pip_tree)`

Writes to `pip_tree` an optimizing solution for `pip`, if it exists.

Querying/Setting Control Parameters

- `int ppl_PIP_Problem_get_control_parameter (ppl_const_PIP_Problem_t pip, int name)`

Returns the value of control parameter `name` in problem `pip`.

- `int ppl_PIP_Problem_set_control_parameter (ppl_PIP_Problem_t pip, int value)`

Sets control parameter `value` in problem `pip`.

Input/Output Functions

- `int ppl_io_print_PIP_Problem (ppl_const_PIP_Problem_t x)`

Prints `x` to `stdout`.

- `int ppl_io_fprint_PIP_Problem (FILE *stream, ppl_const_PIP_Problem_t x)`

Prints `x` to the given output `stream`.

- `int ppl_io_asprint_PIP_Problem (char **strp, ppl_const_PIP_Problem_t x)`

Prints `x` to a malloc-allocated string, a pointer to which is returned via `strp`.

- `int ppl_PIP_Problem_ascii_dump (ppl_const_PIP_Problem_t x, FILE *stream)`

Dumps an ascii representation of `x` on `stream`.

- `int ppl_PIP_Problem_ascii_load (ppl_PIP_Problem_t x, FILE *stream)`

Loads an ascii representation of `x` from `stream`.

7.19.1 Detailed Description

Types and functions for PIP problems.

The types and functions for PIP problems provide an interface towards `PIP_Problem`.

7.19.2 Friends And Related Function Documentation

`int ppl_PIP_Problem_space_dimension (ppl_const_PIP_Problem_t pip, ppl_dimension_type * m)`
[related] Writes to `m` the dimension of the vector space enclosing `pip`.

The vector space dimensions includes both the problem variables and the problem parameters, but they do not include the artificial parameters.

`int ppl_PIP_Problem_add_space_dimensions_and_embed (ppl_PIP_Problem_t pip, ppl_dimension_type pip_vars, ppl_dimension_type pip_params)` **[related]** Adds `pip_vars` + `pip_params` new space dimensions and embeds the PIP problem `pip` in the new vector space.

Parameters

<code>pip</code>	The PIP problem to be embedded in the new vector space.
<code>pip_vars</code>	The number of space dimensions to add that are interpreted as PIP problem variables (i.e., non parameters). These are added <i>before</i> adding the <code>pip_params</code> parameters.
<code>pip_params</code>	The number of space dimensions to add that are interpreted as PIP problem parameters. These are added <i>after</i> having added the <code>pip_vars</code> problem variables.

The new space dimensions will be those having the highest indexes in the new PIP problem; they are initially unconstrained.

int ppl_PIP_Problem_solve (ppl_const_PIP_Problem_t pip) [related] Solves the PIP problem `pip`, returning an exit status.

Returns

`PPL_PIP_PROBLEM_STATUS_UNFEASIBLE` if the PIP problem is not satisfiable; `PPL_PIP_PROBLEM_STATUS_OPTIMIZED` if the PIP problem admits an optimal solution.

The documentation for this interface was generated from the following file:

- `ppl.c.header.h`

7.20 ppl_PIP_Solution_Node_tag Interface Reference

Types and functions for PIP solution nodes.

```
#include <ppl.c.header.h>
```

Related Functions

(Note that these are not member functions.)

- **int ppl_PIP_Solution_Node_get_parametric_values (ppl_const_PIP_Solution_Node_t pip_sol, ppl_dimension_type var, ppl_const_Linear_Expression_t *le)**

Writes to `le` a const pointer to the parametric expression of the values of variable `var` in solution node `pip_sol`.

Input/Output Functions

- **int ppl_io_print_PIP_Solution_Node (ppl_const_PIP_Solution_Node_t x)**
Prints `x` to `stdout`.
- **int ppl_io_fprint_PIP_Solution_Node (FILE *stream, ppl_const_PIP_Solution_Node_t x)**
Prints `x` to the given output `stream`.
- **int ppl_io_asprint_PIP_Solution_Node (char **strp, ppl_const_PIP_Solution_Node_t x)**
Prints `x` to a malloc-allocated string, a pointer to which is returned via `strp`.
- **int ppl_PIP_Solution_Node_ascii_dump (ppl_const_PIP_Solution_Node_t x, FILE *stream)**
Dumps an ascii representation of `x` on `stream`.
- **int ppl_PIP_Solution_Node_ascii_load (ppl_PIP_Solution_Node_t x, FILE *stream)**
Loads an ascii representation of `x` from `stream`.

7.20.1 Detailed Description

Types and functions for PIP solution nodes.

The types and functions for solution nodes provide an interface towards `PIP_Solution_Node`.

7.20.2 Friends And Related Function Documentation

int ppl_PIP_Solution_Node_get_parametric_values (ppl_const_PIP_Solution_Node_t pip_sol, ppl_dimension_type var, ppl_const_Linear_Expression_t *le) [related] Writes to `le` a const pointer to the parametric expression of the values of variable `var` in solution node `pip_sol`.

The linear expression assigned to `le` will only refer to (problem or artificial) parameters.

Parameters

<i>pip_sol</i>	The solution tree node.
<i>var</i>	The variable which is queried about.
<i>le</i>	The returned expression for variable <i>var</i> .

Returns

PPL_ERROR_INVALID_ARGUMENT Returned if *var* is dimension-incompatible with **this* or if *var* is a problem parameter.

The documentation for this interface was generated from the following file:

- `ppl_c_header.h`

7.21 `ppl_PIP_Tree_Node_tag` Interface Reference

Types and functions for generic PIP tree nodes.

```
#include <ppl_c_header.h>
```

Related Functions

(Note that these are not member functions.)

- `int ppl_PIP_Tree_Node_as_solution (ppl_const_PIP_Tree_Node_t pip_tree, ppl_const_PIP_Solution_↔_Node_t *dpipe_tree)`
Writes to *dpipe_tree* the solution node if *pip_tree* is a solution node, and 0 otherwise.
- `int ppl_PIP_Tree_Node_as_decision (ppl_const_PIP_Tree_Node_t pip_tree, ppl_const_PIP_Decision_↔_Node_t *dpipe_tree)`
Writes to *dpipe_tree* the decision node if *pip_tree* is a decision node, and 0 otherwise.
- `int ppl_PIP_Tree_Node_get_constraints (ppl_const_PIP_Tree_Node_t pip_tree, ppl_const_Constraint_↔_System_t *pcs)`
Writes to *pcs* the local system of parameter constraints at the pip tree node *pip_tree*.
- `int ppl_PIP_Tree_Node_OK (ppl_const_PIP_Tree_Node_t pip)`
Returns a positive integer if *pip_tree* is well formed, i.e., if it satisfies all its implementation invariants; returns 0 and perhaps makes some noise if *pip_tree* is broken. Useful for debugging purposes.
- `int ppl_PIP_Tree_Node_number_of_artificials (ppl_const_PIP_Tree_Node_t pip_tree, ppl_dimension_↔_type *m)`
Writes to *m* the number of elements in the artificial parameter sequence in the pip tree node *pip_tree*.
- `int ppl_PIP_Tree_Node_begin (ppl_const_PIP_Tree_Node_t pip_tree, ppl_Artificial_Parameter_Sequence_↔_const_iterator_t pit)`
Assigns to *pit* a const iterator "pointing" to the beginning of the artificial parameter sequence in the pip tree node *pip_tree*.
- `int ppl_PIP_Tree_Node_end (ppl_const_PIP_Tree_Node_t pip_tree, ppl_Artificial_Parameter_Sequence_↔_const_iterator_t pit)`
Assigns to *pit* a const iterator "pointing" to the end of the artificial parameter sequence in the pip tree node *pip_tree*.

Input/Output Functions

- `int ppl_io_print_PIP_Tree_Node (ppl_const_PIP_Tree_Node_t x)`
Prints *x* to *stdout*.
- `int ppl_io_fprint_PIP_Tree_Node (FILE *stream, ppl_const_PIP_Tree_Node_t x)`
Prints *x* to the given output *stream*.
- `int ppl_io_asprint_PIP_Tree_Node (char **strp, ppl_const_PIP_Tree_Node_t x)`

- *Prints x to a malloc-allocated string, a pointer to which is returned via $strp$.*
- `int ppl_PIP_Tree_Node_ascii_dump (ppl_const_PIP_Tree_Node_t x, FILE *stream)`
Dumps an ascii representation of x on $stream$.
- `int ppl_PIP_Tree_Node_ascii_load (ppl_PIP_Tree_Node_t x, FILE *stream)`
Loads an ascii representation of x from $stream$.

7.21.1 Detailed Description

Types and functions for generic PIP tree nodes.

The types and functions for tree nodes provide an interface towards *PIP_Tree_Node*.

The documentation for this interface was generated from the following file:

- `ppl_c_header.h`

7.22 ppl_Pointset_Powerset_C_Polyhedron_const_iterator_tag Interface Reference

Types and functions for iterating on the disjuncts of a const `ppl_Pointset_Powerset_C_Polyhedron_tag`.

Related Functions

(Note that these are not member functions.)

Construction, Initialization and Destruction

- `int ppl_new_Pointset_Powerset_C_Polyhedron_const_iterator (ppl_Pointset_Powerset_C_Polyhedron↔_const_iterator_t *pit)`
Builds a new 'const iterator' and writes a handle to it at address pit .
- `int ppl_new_Pointset_Powerset_C_Polyhedron_const_iterator_from_const_iterator (ppl_Pointset↔_Powerset_C_Polyhedron_const_iterator_t *pit, ppl_const_Pointset_Powerset_C_Polyhedron↔_iterator_t y)`
Builds a copy of y and writes a handle to it at address pit .
- `int ppl_Pointset_Powerset_C_Polyhedron_const_iterator_begin (ppl_const_Pointset_Powerset_C↔_Polyhedron_t ps, ppl_Pointset_Powerset_C_Polyhedron_const_iterator_t psit)`
Assigns to $psit$ a const iterator "pointing" to the beginning of the sequence of disjuncts of ps .
- `int ppl_Pointset_Powerset_C_Polyhedron_const_iterator_end (ppl_const_Pointset_Powerset_C↔_Polyhedron_t ps, ppl_Pointset_Powerset_C_Polyhedron_const_iterator_t psit)`
Assigns to $psit$ a const iterator "pointing" past the end of the sequence of disjuncts of ps .
- `int ppl_delete_Pointset_Powerset_C_Polyhedron_const_iterator (ppl_const_Pointset_Powerset_C↔_Polyhedron_const_iterator_t it)`
Invalidates the handle it : this makes sure the corresponding resources will eventually be released.

Dereferencing, Increment, Decrement and Equality Testing

- `int ppl_Pointset_Powerset_C_Polyhedron_const_iterator_dereference (ppl_const_Pointset_Powerset↔_C_Polyhedron_const_iterator_t it, ppl_const_Polyhedron_t *d)`
Dereferences it writing a const handle to the resulting disjunct at address d .
- `int ppl_Pointset_Powerset_C_Polyhedron_const_iterator_increment (ppl_Pointset_Powerset_C↔_Polyhedron_const_iterator_t it)`
Increments it so that it "points" to the next disjunct.
- `int ppl_Pointset_Powerset_C_Polyhedron_const_iterator_decrement (ppl_Pointset_Powerset_C↔_Polyhedron_const_iterator_t it)`
Decrements it so that it "points" to the previous disjunct.
- `int ppl_Pointset_Powerset_C_Polyhedron_const_iterator_equal_test (ppl_const_Pointset_Powerset↔_C_Polyhedron_const_iterator_t x, ppl_const_Pointset_Powerset_C_Polyhedron_const_iterator_t y)`
Returns a positive integer if the iterators corresponding to x and y are equal; returns 0 if they are different.

7.22.1 Detailed Description

Types and functions for iterating on the disjuncts of a const [ppl_Pointset_Powerset_C_Polyhedron_tag](#).

7.22.2 Friends And Related Function Documentation

int [ppl_Pointset_Powerset_C_Polyhedron_const_iterator_dereference](#) ([ppl_const_Pointset_Powerset_C_Polyhedron_const_iterator_t](#) *it*, [ppl_const_Polyhedron_t](#) * *d*) [**related**] Dereferences *it* writing a const handle to the resulting disjunct at address *d*.

Warning

On exit, the disjunct *d* is still owned by the powerset object: any function call on the owning powerset object may invalidate it. Moreover, *d* should **not** be deleted directly: its resources will be released when deleting the owning powerset.

The documentation for this interface was generated from the following file:

- C_interface.dox

7.23 [ppl_Pointset_Powerset_C_Polyhedron_iterator_tag](#) Interface Reference

Types and functions for iterating on the disjuncts of a [ppl_Pointset_Powerset_C_Polyhedron_tag](#).

Related Functions

(Note that these are not member functions.)

Construction, Initialization and Destruction

- **int** [ppl_new_Pointset_Powerset_C_Polyhedron_iterator](#) ([ppl_Pointset_Powerset_C_Polyhedron_iterator_t](#) **pit*)
*Builds a new 'iterator' and writes a handle to it at address *pit*.*
- **int** [ppl_new_Pointset_Powerset_C_Polyhedron_iterator_from_iterator](#) ([ppl_Pointset_Powerset_C_Polyhedron_iterator_t](#) **pit*, [ppl_const_Pointset_Powerset_C_Polyhedron_iterator_t](#) *y*)
*Builds a copy of *y* and writes a handle to it at address *pit*.*
- **int** [ppl_Pointset_Powerset_C_Polyhedron_iterator_begin](#) ([ppl_Pointset_Powerset_C_Polyhedron_t](#) *ps*, [ppl_Pointset_Powerset_C_Polyhedron_iterator_t](#) *psit*)
*Assigns to *psit* an iterator "pointing" to the beginning of the sequence of disjuncts of *ps*.*
- **int** [ppl_Pointset_Powerset_C_Polyhedron_iterator_end](#) ([ppl_Pointset_Powerset_C_Polyhedron_t](#) *ps*, [ppl_Pointset_Powerset_C_Polyhedron_iterator_t](#) *psit*)
*Assigns to *psit* an iterator "pointing" past the end of the sequence of disjuncts of *ps*.*
- **int** [ppl_delete_Pointset_Powerset_C_Polyhedron_iterator](#) ([ppl_const_Pointset_Powerset_C_Polyhedron_iterator_t](#) *it*)
*Invalidates the handle *it*: this makes sure the corresponding resources will eventually be released.*

Dereferencing, Increment, Decrement and Equality Testing

- **int** [ppl_Pointset_Powerset_C_Polyhedron_iterator_dereference](#) ([ppl_const_Pointset_Powerset_C_Polyhedron_iterator_t](#) *it*, [ppl_const_Polyhedron_t](#) **d*)
*Dereferences *it* writing a const handle to the resulting disjunct at address *d*.*
- **int** [ppl_Pointset_Powerset_C_Polyhedron_iterator_increment](#) ([ppl_Pointset_Powerset_C_Polyhedron_iterator_t](#) *it*)
*Increments *it* so that it "points" to the next disjunct.*
- **int** [ppl_Pointset_Powerset_C_Polyhedron_iterator_decrement](#) ([ppl_Pointset_Powerset_C_Polyhedron_iterator_t](#) *it*)

Decrements `it` so that it "points" to the previous disjunct.

- `int ppl_Pointset_Powerset_C_Polyhedron_iterator_equal_test (ppl_const_Pointset_Powerset_C_Polyhedron_iterator_t x, ppl_const_Pointset_Powerset_C_Polyhedron_iterator_t y)`

Returns a positive integer if the iterators corresponding to `x` and `y` are equal; returns 0 if they are different.

7.23.1 Detailed Description

Types and functions for iterating on the disjuncts of a `ppl_Pointset_Powerset_C_Polyhedron_tag`.

7.23.2 Friends And Related Function Documentation

`int ppl_Pointset_Powerset_C_Polyhedron_iterator_dereference (ppl_const_Pointset_Powerset_C_Polyhedron_iterator_t it, ppl_const_Polyhedron_t * d)` [**related**] Dereferences `it` writing a const handle to the resulting disjunct at address `d`.

Note

Even though `it` is a non-const iterator, dereferencing it results in a handle to a **const** disjunct. This is because mutable iterators are meant to allow for the modification of the sequence of disjuncts (e.g., by dropping elements), while preventing direct modifications of the disjuncts they point to.

Warning

On exit, the disjunct `d` is still owned by the powerset object: any function call on the owning powerset object may invalidate it. Moreover, `d` should **not** be deleted directly: its resources will be released when deleting the owning powerset.

The documentation for this interface was generated from the following file:

- `C_interface.dox`

7.24 `ppl_Pointset_Powerset_C_Polyhedron_tag` Interface Reference

Types and functions for the `Pointset_Powerset` of `C_Polyhedron` objects.

Related Functions

(Note that these are not member functions.)

Ad Hoc Functions for `Pointset_Powerset` domains

- `int ppl_Pointset_Powerset_C_Polyhedron_omega_reduce (ppl_const_Pointset_Powerset_C_Polyhedron_iterator_t ps)`
Drops from the sequence of disjuncts in `ps` all the non-maximal elements so that `ps` is non-redundant.
- `int ppl_Pointset_Powerset_C_Polyhedron_size (ppl_const_Pointset_Powerset_C_Polyhedron_iterator_t ps, size_t *sz)`
Writes to `sz` the number of disjuncts in `ps`.
- `int ppl_Pointset_Powerset_C_Polyhedron_geometrically_covers_Pointset_Powerset_C_Polyhedron (ppl_const_Pointset_Powerset_C_Polyhedron_iterator_t x, ppl_const_Pointset_Powerset_C_Polyhedron_iterator_t y)`
Returns a positive integer if powerset `x` geometrically covers powerset `y`; returns 0 otherwise.
- `int ppl_Pointset_Powerset_C_Polyhedron_geometrically_equals_Pointset_Powerset_C_Polyhedron (ppl_const_Pointset_Powerset_C_Polyhedron_iterator_t x, ppl_const_Pointset_Powerset_C_Polyhedron_iterator_t y)`
Returns a positive integer if powerset `x` is geometrically equal to powerset `y`; returns 0 otherwise.
- `int ppl_Pointset_Powerset_C_Polyhedron_add_disjunct (ppl_Pointset_Powerset_C_Polyhedron_iterator_t ps, ppl_const_Polyhedron_iterator_t d)`

- Adds to `ps` a copy of disjunct `d`.*

 - `int ppl_Pointset_Powerset_C_Polyhedron_drop_disjunct (ppl_Pointset_Powerset_C_Polyhedron_t ps, ppl_const_Pointset_Powerset_C_Polyhedron_iterator_t cit, ppl_Pointset_Powerset_C_Polyhedron_iterator_t it)`

Drops from `ps` the disjunct pointed to by `cit`, assigning to `it` an iterator to the disjunct following `cit`.
- `int ppl_Pointset_Powerset_C_Polyhedron_drop_disjuncts (ppl_Pointset_Powerset_C_Polyhedron_t ps, ppl_const_Pointset_Powerset_C_Polyhedron_iterator_t first, ppl_const_Pointset_Powerset_C_Polyhedron_iterator_t last)`

Drops from `ps` all the disjuncts from `first` to `last` (excluded).
- `int ppl_Pointset_Powerset_C_Polyhedron_pairwise_reduce (ppl_Pointset_Powerset_C_Polyhedron_t ps)`

Modifies `ps` by (recursively) merging together the pairs of disjuncts whose upper-bound is the same as their set-theoretical union.

7.24.1 Detailed Description

Types and functions for the Pointset_Powerset of C_Polyhedron objects.

The powerset domains can be instantiated by taking as a base domain any fixed semantic geometric description (C and NNC polyhedra, BD and octagonal shapes, boxes and grids). An element of the powerset domain represents a disjunctive collection of base objects (its disjuncts), all having the same space dimension.

Besides the functions that are available in all semantic geometric descriptions (whose documentation is not repeated here), the powerset domain also provides several ad hoc functions. In particular, the iterator types allow for the examination and manipulation of the collection of disjuncts.

7.24.2 Friends And Related Function Documentation

`int ppl_Pointset_Powerset_C_Polyhedron_size (ppl_const_Pointset_Powerset_C_Polyhedron_t ps, size_t * sz)` [**related**] Writes to `sz` the number of disjuncts in `ps`.

Note

If present, Omega-redundant elements will be counted too.

The documentation for this interface was generated from the following file:

- C_interface.dox

7.25 ppl_Polyhedron_tag Interface Reference

Types and functions for the domains of C and NNC convex polyhedra.

Related Functions

(Note that these are not member functions.)

Constructors and Assignment for C_Polyhedron

- `int ppl_new_C_Polyhedron_from_space_dimension (ppl_Polyhedron_t *pph, ppl_dimension_type d, int empty)`

Builds a C polyhedron of dimension `d` and writes an handle to it at address `pph`. If `empty` is different from zero, the newly created polyhedron will be empty; otherwise, it will be a universe polyhedron.
- `int ppl_new_C_Polyhedron_from_C_Polyhedron (ppl_Polyhedron_t *pph, ppl_const_Polyhedron_t ph)`

Builds a C polyhedron that is a copy of `ph`; writes a handle for the newly created polyhedron at address `pph`.

- `int ppl_new_C_Polyhedron_from_C_Polyhedron_with_complexity (ppl_Polyhedron_t *pph, ppl_const_Polyhedron_t ph, int complexity)`
Builds a C polyhedron that is a copy of `ph`; writes a handle for the newly created polyhedron at address `pph`.
- `int ppl_new_C_Polyhedron_from_Constraint_System (ppl_Polyhedron_t *pph, ppl_const_Constraint_System_t cs)`
Builds a new C polyhedron from the system of constraints `cs` and writes a handle for the newly created polyhedron at address `pph`.
- `int ppl_new_C_Polyhedron_recycle_Constraint_System (ppl_Polyhedron_t *pph, ppl_Constraint_System_t cs)`
Builds a new C polyhedron recycling the system of constraints `cs` and writes a handle for the newly created polyhedron at address `pph`.
- `int ppl_new_C_Polyhedron_from_Congruence_System (ppl_Polyhedron_t *pph, ppl_const_Congruence_System_t cs)`
Builds a new C polyhedron from the system of congruences `cs` and writes a handle for the newly created polyhedron at address `pph`.
- `int ppl_new_C_Polyhedron_recycle_Congruence_System (ppl_Polyhedron_t *pph, ppl_Congruence_System_t cs)`
Builds a new C polyhedron recycling the system of congruences `cs` and writes a handle for the newly created polyhedron at address `pph`.
- `int ppl_assign_C_Polyhedron_from_C_Polyhedron (ppl_Polyhedron_t dst, ppl_const_Polyhedron_t src)`
Assigns a copy of the C polyhedron `src` to the C polyhedron `dst`.

Constructors and Assignment for NNC_Polyhedron

- `int ppl_new_NNC_Polyhedron_from_space_dimension (ppl_Polyhedron_t *pph, ppl_dimension_type d, int empty)`
Builds an NNC polyhedron of dimension `d` and writes an handle to it at address `pph`. If `empty` is different from zero, the newly created polyhedron will be empty; otherwise, it will be a universe polyhedron.
- `int ppl_new_NNC_Polyhedron_from_NNC_Polyhedron (ppl_Polyhedron_t *pph, ppl_const_Polyhedron_t ph)`
Builds an NNC polyhedron that is a copy of `ph`; writes a handle for the newly created polyhedron at address `pph`.
- `int ppl_new_NNC_Polyhedron_from_NNC_Polyhedron_with_complexity (ppl_Polyhedron_t *pph, ppl_const_Polyhedron_t ph, int complexity)`
Builds an NNC polyhedron that is a copy of `ph`; writes a handle for the newly created polyhedron at address `pph`.
- `int ppl_new_NNC_Polyhedron_from_Constraint_System (ppl_Polyhedron_t *pph, ppl_const_Constraint_System_t cs)`
Builds a new NNC polyhedron from the system of constraints `cs` and writes a handle for the newly created polyhedron at address `pph`.
- `int ppl_new_NNC_Polyhedron_recycle_Constraint_System (ppl_Polyhedron_t *pph, ppl_Constraint_System_t cs)`
Builds a new NNC polyhedron recycling the system of constraints `cs` and writes a handle for the newly created polyhedron at address `pph`.
- `int ppl_new_NNC_Polyhedron_from_Congruence_System (ppl_Polyhedron_t *pph, ppl_const_Congruence_System_t cs)`
Builds a new NNC polyhedron from the system of congruences `cs` and writes a handle for the newly created polyhedron at address `pph`.
- `int ppl_new_NNC_Polyhedron_recycle_Congruence_System (ppl_Polyhedron_t *pph, ppl_Congruence_System_t cs)`
Builds a new NNC polyhedron recycling the system of congruences `cs` and writes a handle for the newly created polyhedron at address `pph`.

- `int ppl_assign_NNC_Polyhedron_from_NNC_Polyhedron (ppl_Polyhedron_t dst, ppl_const_Polyhedron_t src)`

Assigns a copy of the NNC polyhedron `src` to the NNC polyhedron `dst`.

Constructors Behaving as Conversion Operators

Besides the conversions listed here below, the library also provides conversion operators that build a semantic geometric description starting from **any** other semantic geometric description (e.g., `ppl_new_Grid_from_C_Polyhedron`, `ppl_new_C_Polyhedron_from_BD_Shape_mpq_class`, etc.). Clearly, the conversion operators are only available if both the source and the target semantic geometric descriptions have been enabled when configuring the library. The conversions also taking as argument a complexity class sometimes provide non-trivial precision/efficiency trade-offs.

- `int ppl_new_C_Polyhedron_from_NNC_Polyhedron (ppl_Polyhedron_t *pph, ppl_const_Polyhedron_t ph)`
Builds a C polyhedron that is a copy of the topological closure of the NNC polyhedron `ph`; writes a handle for the newly created polyhedron at address `pph`.
- `int ppl_new_C_Polyhedron_from_NNC_Polyhedron_with_complexity (ppl_Polyhedron_t *pph, ppl_const_Polyhedron_t ph, int complexity)`
Builds a C polyhedron that approximates NNC_Polyhedron `ph`, using an algorithm whose complexity does not exceed `complexity`; writes a handle for the newly created polyhedron at address `pph`.
- `int ppl_new_NNC_Polyhedron_from_C_Polyhedron (ppl_Polyhedron_t *pph, ppl_const_Polyhedron_t ph)`
Builds an NNC polyhedron that is a copy of the C polyhedron `ph`; writes a handle for the newly created polyhedron at address `pph`.
- `int ppl_new_NNC_Polyhedron_from_C_Polyhedron_with_complexity (ppl_Polyhedron_t *pph, ppl_const_Polyhedron_t ph, int complexity)`
Builds an NNC polyhedron that approximates C_Polyhedron `ph`, using an algorithm whose complexity does not exceed `complexity`; writes a handle for the newly created polyhedron at address `pph`.

Destructor for (C or NNC) Polyhedra

- `int ppl_delete_Polyhedron (ppl_const_Polyhedron_t ph)`
Invalidates the handle `ph`: this makes sure the corresponding resources will eventually be released.

Functions that Do Not Modify the Polyhedron

- `int ppl_Polyhedron_space_dimension (ppl_const_Polyhedron_t ph, ppl_dimension_type *m)`
Writes to `m` the dimension of the vector space enclosing `ph`.
- `int ppl_Polyhedron_affine_dimension (ppl_const_Polyhedron_t ph, ppl_dimension_type *m)`
Writes to `m` the affine dimension of `ph` (not to be confused with the dimension of its enclosing vector space) or 0, if `ph` is empty.
- `int ppl_Polyhedron_relation_with_Constraint (ppl_const_Polyhedron_t ph, ppl_const_Constraint_t c)`
Checks the relation between the polyhedron `ph` and the constraint `c`.
- `int ppl_Polyhedron_relation_with_Generator (ppl_const_Polyhedron_t ph, ppl_const_Generator_t g)`
Checks the relation between the polyhedron `ph` and the generator `g`.
- `int ppl_Polyhedron_get_constraints (ppl_const_Polyhedron_t ph, ppl_const_Constraint_System_t *pcs)`
Writes a const handle to the constraint system defining the polyhedron `ph` at address `pcs`.
- `int ppl_Polyhedron_get_congruences (ppl_const_Polyhedron_t ph, ppl_const_Congruence_System_t *pcs)`
Writes at address `pcs` a const handle to a system of congruences approximating the polyhedron `ph`.
- `int ppl_Polyhedron_get_minimized_constraints (ppl_const_Polyhedron_t ph, ppl_const_Constraint_System_t *pcs)`

- Writes a const handle to the minimized constraint system defining the polyhedron ph at address pcs .*
- `int ppl_Polyhedron_get_minimized_congruences (ppl_const_Polyhedron_t ph, ppl_const_Congruence↔_System_t *pcs)`
Writes at address pcs a const handle to a system of minimized congruences approximating the polyhedron ph .
- `int ppl_Polyhedron_is_empty (ppl_const_Polyhedron_t ph)`
Returns a positive integer if ph is empty; returns 0 if ph is not empty.
- `int ppl_Polyhedron_is_universe (ppl_const_Polyhedron_t ph)`
Returns a positive integer if ph is a universe polyhedron; returns 0 if it is not.
- `int ppl_Polyhedron_is_bounded (ppl_const_Polyhedron_t ph)`
Returns a positive integer if ph is bounded; returns 0 if ph is unbounded.
- `int ppl_Polyhedron_contains_integer_point (ppl_const_Polyhedron_t ph)`
Returns a positive integer if ph contains at least one integer point; returns 0 otherwise.
- `int ppl_Polyhedron_is_topologically_closed (ppl_const_Polyhedron_t ph)`
Returns a positive integer if ph is topologically closed; returns 0 if ph is not topologically closed.
- `int ppl_Polyhedron_is_discrete (ppl_const_Polyhedron_t ph)`
Returns a positive integer if ph is a discrete set; returns 0 if ph is not a discrete set.
- `int ppl_Polyhedron_constrains (ppl_Polyhedron_t ph, ppl_dimension_type var)`
Returns a positive integer if ph constrains var ; returns 0 if ph does not constrain var .
- `int ppl_Polyhedron_bounds_from_above (ppl_const_Polyhedron_t ph, ppl_const_Linear_Expression↔_t le)`
Returns a positive integer if le is bounded from above in ph ; returns 0 otherwise.
- `int ppl_Polyhedron_bounds_from_below (ppl_const_Polyhedron_t ph, ppl_const_Linear_Expression↔_t le)`
Returns a positive integer if le is bounded from below in ph ; returns 0 otherwise.
- `int ppl_Polyhedron_maximize_with_point (ppl_const_Polyhedron_t ph, ppl_const_Linear_Expression↔_t le, ppl_Coefficient_t sup_n, ppl_Coefficient_t sup_d, int *pmaximum, ppl_Generator_t point)`
Returns a positive integer if ph is not empty and le is bounded from above in ph , in which case the supremum value and a point where le reaches it are computed.
- `int ppl_Polyhedron_maximize (ppl_const_Polyhedron_t ph, ppl_const_Linear_Expression_t le, ppl↔_Coefficient_t sup_n, ppl_Coefficient_t sup_d, int *pmaximum)`
The same as `ppl_Polyhedron_maximize_with_point`, but without the output argument for the location where the supremum value is reached.
- `int ppl_Polyhedron_minimize_with_point (ppl_const_Polyhedron_t ph, ppl_const_Linear_Expression↔_t le, ppl_Coefficient_t inf_n, ppl_Coefficient_t inf_d, int *pminimum, ppl_Generator_t point)`
Returns a positive integer if ph is not empty and le is bounded from below in ph , in which case the infimum value and a point where le reaches it are computed.
- `int ppl_Polyhedron_minimize_with_point (ppl_const_Polyhedron_t ph, ppl_const_Linear_Expression↔_t le, ppl_Coefficient_t inf_n, ppl_Coefficient_t inf_d, int *pminimum)`
The same as `ppl_Polyhedron_minimize_with_point`, but without the output argument for the location where the infimum value is reached.
- `int ppl_Polyhedron_contains_Polyhedron (ppl_const_Polyhedron_t x, ppl_const_Polyhedron_t y)`
Returns a positive integer if x contains or is equal to y ; returns 0 if it does not.
- `int ppl_Polyhedron_strictly_contains_Polyhedron (ppl_const_Polyhedron_t x, ppl_const_Polyhedron↔_t y)`
Returns a positive integer if x strictly contains y ; returns 0 if it does not.
- `int ppl_Polyhedron_is_disjoint_from_Polyhedron (ppl_const_Polyhedron_t x, ppl_const_Polyhedron↔_t y)`
Returns a positive integer if x and y are disjoint; returns 0 if they are not.
- `int ppl_Polyhedron_equals_Polyhedron (ppl_const_Polyhedron_t x, ppl_const_Polyhedron_t y)`
Returns a positive integer if x and y are the same polyhedron; returns 0 if they are different.
- `int ppl_Polyhedron_OK (ppl_const_Polyhedron_t ph)`

Returns a positive integer if ph is well formed, i.e., if it satisfies all its implementation invariants; returns 0 and perhaps makes some noise if ph is broken. Useful for debugging purposes.

- int `ppl_Polyhedron_external_memory_in_bytes` (`ppl_const_Polyhedron_t` ph , `size_t` $*sz$)
Writes to sz a lower bound to the size in bytes of the memory managed by ph .
- int `ppl_Polyhedron_total_memory_in_bytes` (`ppl_const_Polyhedron_t` ph , `size_t` $*sz$)
Writes to sz a lower bound to the size in bytes of the memory managed by ph .

Space Dimension Preserving Functions that May Modify the Polyhedron

- int `ppl_Polyhedron_add_constraint` (`ppl_Polyhedron_t` ph , `ppl_const_Constraint_t` c)
Adds a copy of the constraint c to the system of constraints of ph .
- int `ppl_Polyhedron_add_congruence` (`ppl_Polyhedron_t` ph , `ppl_const_Congruence_t` c)
Adds a copy of the congruence c to polyhedron of ph .
- int `ppl_Polyhedron_add_constraints` (`ppl_Polyhedron_t` ph , `ppl_const_Constraint_System_t` cs)
Adds a copy of the system of constraints cs to the system of constraints of ph .
- int `ppl_Polyhedron_add_congruences` (`ppl_Polyhedron_t` ph , `ppl_const_Congruence_System_t` cs)
Adds a copy of the system of congruences cs to the polyhedron ph .
- int `ppl_Polyhedron_add_recycled_constraints` (`ppl_Polyhedron_t` ph , `ppl_Constraint_System_t` cs)
Adds the system of constraints cs to the system of constraints of ph .
- int `ppl_Polyhedron_add_recycled_congruences` (`ppl_Polyhedron_t` ph , `ppl_Congruence_System_t` cs)
Adds the system of congruences cs to the polyhedron ph .
- int `ppl_Polyhedron_refine_with_constraint` (`ppl_Polyhedron_t` ph , `ppl_const_Constraint_t` c)
Refines ph using constraint c .
- int `ppl_Polyhedron_refine_with_congruence` (`ppl_Polyhedron_t` ph , `ppl_const_Congruence_t` c)
Refines ph using congruence c .
- int `ppl_Polyhedron_refine_with_constraints` (`ppl_Polyhedron_t` ph , `ppl_const_Constraint_System_t` cs)
Refines ph using the constraints in cs .
- int `ppl_Polyhedron_refine_with_congruences` (`ppl_Polyhedron_t` ph , `ppl_const_Congruence_System_t` cs)
Refines ph using the congruences in cs .
- int `ppl_Polyhedron_intersection_assign` (`ppl_Polyhedron_t` x , `ppl_const_Polyhedron_t` y)
Intersects x with polyhedron y and assigns the result to x .
- int `ppl_Polyhedron_upper_bound_assign` (`ppl_Polyhedron_t` x , `ppl_const_Polyhedron_t` y)
Assigns to x an upper bound of x and y .
- int `ppl_Polyhedron_difference_assign` (`ppl_Polyhedron_t` x , `ppl_const_Polyhedron_t` y)
Same as `ppl_Polyhedron_poly_difference_assign(x, y)`.
- int `ppl_Polyhedron_simplify_using_context_assign` (`ppl_Polyhedron_t` x , `ppl_const_Polyhedron_t` y)
Assigns to x the meet-preserving simplification of x with respect to context y . Returns a positive integer if x and y have a nonempty intersection; returns 0 if they are disjoint.
- int `ppl_Polyhedron_time_elapse_assign` (`ppl_Polyhedron_t` x , `ppl_const_Polyhedron_t` y)
Assigns to x the time-elapse between the polyhedra x and y .
- int `ppl_Polyhedron_topological_closure_assign` (`ppl_Polyhedron_t` ph)
Assigns to ph its topological closure.
- int `ppl_Polyhedron_unconstrain_space_dimension` (`ppl_Polyhedron_t` ph , `ppl_dimension_type` var)
Modifies ph by unconstraining the space dimension var .
- int `ppl_Polyhedron_unconstrain_space_dimensions` (`ppl_Polyhedron_t` ph , `ppl_dimension_type` $ds[]$, `size_t` n)
Modifies ph by unconstraining the space dimensions that are specified in the first n positions of the array ds . The presence of duplicates in ds is a waste but an innocuous one.
- int `ppl_Polyhedron_affine_image` (`ppl_Polyhedron_t` ph , `ppl_dimension_type` var , `ppl_const_Linear_Expression_t` le , `ppl_const_Coefficient_t` d)

- Transforms the polyhedron ph , assigning an affine expression to the specified variable.*

• int `ppl_Polyhedron_affine_preimage` (`ppl_Polyhedron_t` ph , `ppl_dimension_type` var , `ppl_const_linear_Expression_t` le , `ppl_const_Coefficient_t` d)
- Transforms the polyhedron ph , substituting an affine expression to the specified variable.*

• int `ppl_Polyhedron_bounded_affine_image` (`ppl_Polyhedron_t` ph , `ppl_dimension_type` var , `ppl_const_linear_Expression_t` lb , `ppl_const_linear_Expression_t` ub , `ppl_const_Coefficient_t` d)

Assigns to ph the image of ph with respect to the generalized affine transfer relation $\frac{lb}{d} \leq var' \leq \frac{ub}{d}$.
- int `ppl_Polyhedron_bounded_affine_preimage` (`ppl_Polyhedron_t` ph , `ppl_dimension_type` var , `ppl_const_linear_Expression_t` lb , `ppl_const_linear_Expression_t` ub , `ppl_const_Coefficient_t` d)

Assigns to ph the preimage of ph with respect to the generalized affine transfer relation $\frac{lb}{d} \leq var' \leq \frac{ub}{d}$.
- int `ppl_Polyhedron_generalized_affine_image` (`ppl_Polyhedron_t` ph , `ppl_dimension_type` var , `enum_ppl_enum_Constraint_Type` $relysym$, `ppl_const_linear_Expression_t` le , `ppl_const_Coefficient_t` d)

Assigns to ph the image of ph with respect to the generalized affine transfer relation $var' \bowtie \frac{le}{d}$, where \bowtie is the relation symbol encoded by `relysym`.
- int `ppl_Polyhedron_generalized_affine_preimage` (`ppl_Polyhedron_t` ph , `ppl_dimension_type` var , `enum_ppl_enum_Constraint_Type` $relysym$, `ppl_const_linear_Expression_t` le , `ppl_const_Coefficient_t` d)

Assigns to ph the preimage of ph with respect to the generalized affine transfer relation $var' \bowtie \frac{le}{d}$, where \bowtie is the relation symbol encoded by `relysym`.
- int `ppl_Polyhedron_generalized_affine_image_lhs_rhs` (`ppl_Polyhedron_t` ph , `ppl_const_linear_Expression_t` lhs , `enum_ppl_enum_Constraint_Type` $relysym$, `ppl_const_linear_Expression_t` rhs)

Assigns to ph the image of ph with respect to the generalized affine transfer relation $lhs' \bowtie rhs$, where \bowtie is the relation symbol encoded by `relysym`.
- int `ppl_Polyhedron_generalized_affine_preimage_lhs_rhs` (`ppl_Polyhedron_t` ph , `ppl_const_linear_Expression_t` lhs , `enum_ppl_enum_Constraint_Type` $relysym$, `ppl_const_linear_Expression_t` rhs)

Assigns to ph the preimage of ph with respect to the generalized affine transfer relation $lhs' \bowtie rhs$, where \bowtie is the relation symbol encoded by `relysym`.

Functions that May Modify the Dimension of the Vector Space

- int `ppl_Polyhedron_concatenate_assign` (`ppl_Polyhedron_t` x , `ppl_const_Polyhedron_t` y)

Seeing a polyhedron as a set of tuples (its points), assigns to x all the tuples that can be obtained by concatenating, in the order given, a tuple of x with a tuple of y .
- int `ppl_Polyhedron_add_space_dimensions_and_embed` (`ppl_Polyhedron_t` ph , `ppl_dimension_type` d)

Adds d new dimensions to the space enclosing the polyhedron ph and to ph itself.
- int `ppl_Polyhedron_add_space_dimensions_and_project` (`ppl_Polyhedron_t` ph , `ppl_dimension_type` d)

Adds d new dimensions to the space enclosing the polyhedron ph .
- int `ppl_Polyhedron_remove_space_dimensions` (`ppl_Polyhedron_t` ph , `ppl_dimension_type` ds [], `size_t` n)

Removes from the vector space enclosing ph the space dimensions that are specified in first n positions of the array ds . The presence of duplicates in ds is a waste but an innocuous one.
- int `ppl_Polyhedron_remove_higher_space_dimensions` (`ppl_Polyhedron_t` ph , `ppl_dimension_type` d)

Removes the higher dimensions from the vector space enclosing ph so that, upon successful return, the new space dimension is d .
- int `ppl_Polyhedron_map_space_dimensions` (`ppl_Polyhedron_t` ph , `ppl_dimension_type` $maps$ [], `size_t` n)

Remaps the dimensions of the vector space according to a partial function. This function is specified by means of the `maps` array, which has n entries.
- int `ppl_Polyhedron_expand_space_dimension` (`ppl_Polyhedron_t` ph , `ppl_dimension_type` d , `ppl_dimension_type` m)

Expands the d -th dimension of the vector space enclosing ph to m new space dimensions.

- int `ppl_Polyhedron_fold_space_dimensions` (`ppl_Polyhedron_t` `ph`, `ppl_dimension_type` `ds[]`, `size_t` `n`, `ppl_dimension_type` `d`)
Modifies `ph` by folding the space dimensions contained in the first `n` positions of the array `ds` into dimension `d`. The presence of duplicates in `ds` is a waste but an innocuous one.

Input/Output Functions

- int `ppl_io_print_Polyhedron` (`ppl_const_Polyhedron_t` `x`)
Prints `x` to `stdout`.
- int `ppl_io_fprint_Polyhedron` (`FILE` `*stream`, `ppl_const_Polyhedron_t` `x`)
Prints `x` to the given output `stream`.
- int `ppl_io_asprint_Polyhedron` (`char**strp`, `ppl_const_Polyhedron_t` `x`)
Prints `x` to a malloc-allocated string, a pointer to which is returned via `strp`.
- int `ppl_Polyhedron_ascii_dump` (`ppl_const_Polyhedron_t` `x`, `FILE` `*stream`)
Dumps an ascii representation of `x` on `stream`.
- int `ppl_Polyhedron_ascii_load` (`ppl_Polyhedron_t` `x`, `FILE` `*stream`)
Loads an ascii representation of `x` from `stream`.

Ad Hoc Functions for (C or NNC) Polyhedra

The functions listed here below, being specific of the polyhedron domains, do not have a correspondence in other semantic geometric descriptions.

- int `ppl_new_C_Polyhedron_from_Generator_System` (`ppl_Polyhedron_t` `*pph`, `ppl_const_Generator_System_t` `gs`)
Builds a new C polyhedron from the system of generators `gs` and writes a handle for the newly created polyhedron at address `pph`.
- int `ppl_new_C_Polyhedron_recycle_Generator_System` (`ppl_Polyhedron_t` `*pph`, `ppl_Generator_System_t` `gs`)
Builds a new C polyhedron recycling the system of generators `gs` and writes a handle for the newly created polyhedron at address `pph`.
- int `ppl_new_NNC_Polyhedron_from_Generator_System` (`ppl_Polyhedron_t` `*pph`, `ppl_const_Generator_System_t` `gs`)
Builds a new NNC polyhedron from the system of generators `gs` and writes a handle for the newly created polyhedron at address `pph`.
- int `ppl_new_NNC_Polyhedron_recycle_Generator_System` (`ppl_Polyhedron_t` `*pph`, `ppl_Generator_System_t` `gs`)
Builds a new NNC polyhedron recycling the system of generators `gs` and writes a handle for the newly created polyhedron at address `pph`.
- int `ppl_Polyhedron_get_generators` (`ppl_const_Polyhedron_t` `ph`, `ppl_const_Generator_System_t` `*pgs`)
Writes a const handle to the generator system defining the polyhedron `ph` at address `pgs`.
- int `ppl_Polyhedron_get_minimized_generators` (`ppl_const_Polyhedron_t` `ph`, `ppl_const_Generator_System_t` `*pgs`)
Writes a const handle to the minimized generator system defining the polyhedron `ph` at address `pgs`.
- int `ppl_Polyhedron_add_generator` (`ppl_Polyhedron_t` `ph`, `ppl_const_Generator_t` `g`)
Adds a copy of the generator `g` to the system of generators of `ph`.
- int `ppl_Polyhedron_add_generators` (`ppl_Polyhedron_t` `ph`, `ppl_const_Generator_System_t` `gs`)
Adds a copy of the system of generators `gs` to the system of generators of `ph`.
- int `ppl_Polyhedron_add_recycled_generators` (`ppl_Polyhedron_t` `ph`, `ppl_Generator_System_t` `gs`)
Adds the system of generators `gs` to the system of generators of `ph`.
- int `ppl_Polyhedron_poly_hull_assign` (`ppl_Polyhedron_t` `x`, `ppl_const_Polyhedron_t` `y`)
Assigns to `x` the poly-hull of `x` and `y`.
- int `ppl_Polyhedron_poly_difference_assign` (`ppl_Polyhedron_t` `x`, `ppl_const_Polyhedron_t` `y`)
Assigns to `x` the poly-difference of `x` and `y`.

- `int wrap_assign (ppl.Polyhedron_t ph, ppl.dimension_type ds[], size_t n, ppl_enum_Bounded_Integer_Type_Width w, ppl_enum_Bounded_Integer_Type_Representation r, ppl_enum_Bounded_Integer_Type_Overflow o, const ppl_const_Constraint_System_t *pcs, unsigned complexity_threshold, int wrap_individually)`
Assigns to `ph` the polyhedron obtained from `ph` by "wrapping" the vector space defined by the first `n` space dimensions in `ds[]`.
- `int ppl_Polyhedron_BHRZ03_widening_assign_with_tokens (ppl.Polyhedron_t x, ppl_const_Polyhedron_t y, unsigned *tp)`
*If the polyhedron `y` is contained in (or equal to) the polyhedron `x`, assigns to `x` the BHRZ03-widening of `x` and `y`. If `tp` is not the null pointer, the widening with tokens delay technique is applied with `*tp` available tokens.*
- `int ppl_Polyhedron_H79_widening_assign_with_tokens (ppl.Polyhedron_t x, ppl_const_Polyhedron_t y, unsigned *tp)`
*If the polyhedron `y` is contained in (or equal to) the polyhedron `x`, assigns to `x` the H79-widening of `x` and `y`. If `tp` is not the null pointer, the widening with tokens delay technique is applied with `*tp` available tokens.*
- `int ppl_Polyhedron_BHRZ03_widening_assign (ppl.Polyhedron_t x, ppl_const_Polyhedron_t y)`
If the polyhedron `y` is contained in (or equal to) the polyhedron `x`, assigns to `x` the BHRZ03-widening of `x` and `y`.
- `int ppl_Polyhedron_H79_widening_assign (ppl.Polyhedron_t x, ppl_const_Polyhedron_t y)`
If the polyhedron `y` is contained in (or equal to) the polyhedron `x`, assigns to `x` the H79-widening of `x` and `y`.
- `int ppl_Polyhedron_limited_BHRZ03_extrapolation_assign_with_tokens (ppl.Polyhedron_t x, ppl_const_Polyhedron_t y, ppl_const_Constraint_System_t cs, unsigned *tp)`
*If the polyhedron `y` is contained in (or equal to) the polyhedron `x`, assigns to `x` the BHRZ03-widening of `x` and `y` intersected with the constraints in `cs` that are satisfied by all the points of `x`. If `tp` is not the null pointer, the widening with tokens delay technique is applied with `*tp` available tokens.*
- `int ppl_Polyhedron_limited_H79_extrapolation_assign_with_tokens (ppl.Polyhedron_t x, ppl_const_Polyhedron_t y, ppl_const_Constraint_System_t cs, unsigned *tp)`
*If the polyhedron `y` is contained in (or equal to) the polyhedron `x`, assigns to `x` the H79-widening of `x` and `y` intersected with the constraints in `cs` that are satisfied by all the points of `x`. If `tp` is not the null pointer, the widening with tokens delay technique is applied with `*tp` available tokens.*
- `int ppl_Polyhedron_limited_BHRZ03_extrapolation_assign (ppl.Polyhedron_t x, ppl_const_Polyhedron_t y, ppl_const_Constraint_System_t cs)`
If the polyhedron `y` is contained in (or equal to) the polyhedron `x`, assigns to `x` the BHRZ03-widening of `x` and `y` intersected with the constraints in `cs` that are satisfied by all the points of `x`.
- `int ppl_Polyhedron_limited_H79_extrapolation_assign (ppl.Polyhedron_t x, ppl_const_Polyhedron_t y, ppl_const_Constraint_System_t cs)`
If the polyhedron `y` is contained in (or equal to) the polyhedron `x`, assigns to `x` the H79-widening of `x` and `y` intersected with the constraints in `cs` that are satisfied by all the points of `x`.
- `int ppl_Polyhedron_bounded_BHRZ03_extrapolation_assign_with_tokens (ppl.Polyhedron_t x, ppl_const_Polyhedron_t y, ppl_const_Constraint_System_t cs, unsigned *tp)`
*If the polyhedron `y` is contained in (or equal to) the polyhedron `x`, assigns to `x` the BHRZ03-widening of `x` and `y` intersected with the constraints in `cs` that are satisfied by all the points of `x`, further intersected with all the constraints of the form $\pm v \leq r$ and $\pm v < r$, with $r \in \mathbb{Q}$, that are satisfied by all the points of `x`. If `tp` is not the null pointer, the widening with tokens delay technique is applied with `*tp` available tokens.*
- `int ppl_Polyhedron_bounded_H79_extrapolation_assign_with_tokens (ppl.Polyhedron_t x, ppl_const_Polyhedron_t y, ppl_const_Constraint_System_t cs, unsigned *tp)`
*If the polyhedron `y` is contained in (or equal to) the polyhedron `x`, assigns to `x` the H79-widening of `x` and `y` intersected with the constraints in `cs` that are satisfied by all the points of `x`, further intersected with all the constraints of the form $\pm v \leq r$ and $\pm v < r$, with $r \in \mathbb{Q}$, that are satisfied by all the points of `x`. If `tp` is not the null pointer, the widening with tokens delay technique is applied with `*tp` available tokens.*

- `int ppl_Polyhedron_bounded_BHRZ03_extrapolation_assign (ppl_Polyhedron_t x, ppl_const_Polyhedron_t y, ppl_const_Constraint_System_t cs)`
If the polyhedron y is contained in (or equal to) the polyhedron x , assigns to x the BHRZ03-widening of x and y intersected with the constraints in cs that are satisfied by all the points of x , further intersected with all the constraints of the form $\pm v \leq r$ and $\pm v < r$, with $r \in \mathbb{Q}$, that are satisfied by all the points of x .
- `int ppl_Polyhedron_bounded_H79_extrapolation_assign (ppl_Polyhedron_t x, ppl_const_Polyhedron_t y, ppl_const_Constraint_System_t cs)`
If the polyhedron y is contained in (or equal to) the polyhedron x , assigns to x the H79-widening of x and y intersected with the constraints in cs that are satisfied by all the points of x , further intersected with all the constraints of the form $\pm v \leq r$ and $\pm v < r$, with $r \in \mathbb{Q}$, that are satisfied by all the points of x .

7.25.1 Detailed Description

Types and functions for the domains of C and NNC convex polyhedra.

The types and functions for convex polyhedra provide a single interface for accessing both topologically closed (C) and not necessarily closed (NNC) convex polyhedra. The distinction between C and NNC polyhedra need only be explicitly stated when *creating* or *assigning* a polyhedron object, by means of one of the functions `ppl_new_*` and `ppl_assign_*`.

Having a single datatype does not mean that C and NNC polyhedra can be freely interchanged: as specified in the main manual, most library functions require their arguments to be topologically and/or space-dimension compatible.

7.25.2 Friends And Related Function Documentation

`int ppl_new_C_Polyhedron_from_C_Polyhedron_with_complexity (ppl_Polyhedron_t * pph, ppl_const_Polyhedron_t ph, int complexity) [related]` Builds a C polyhedron that is a copy of `ph`; writes a handle for the newly created polyhedron at address `pph`.

Note

The complexity argument is ignored.

`int ppl_new_C_Polyhedron_from_Constraint_System (ppl_Polyhedron_t * pph, ppl_const_Constraint_System_t cs) [related]` Builds a new C polyhedron from the system of constraints `cs` and writes a handle for the newly created polyhedron at address `pph`.

The new polyhedron will inherit the space dimension of `cs`.

`int ppl_new_C_Polyhedron_recycle_Constraint_System (ppl_Polyhedron_t * pph, ppl_Constraint_System_t cs) [related]` Builds a new C polyhedron recycling the system of constraints `cs` and writes a handle for the newly created polyhedron at address `pph`.

The new polyhedron will inherit the space dimension of `cs`.

Warning

This function modifies the constraint system referenced by `cs`: upon return, no assumption can be made on its value.

`int ppl_new_C_Polyhedron_from_Congruence_System (ppl_Polyhedron_t * pph, ppl_const_Congruence_System_t cs) [related]` Builds a new C polyhedron from the system of congruences `cs` and writes a handle for the newly created polyhedron at address `pph`.

The new polyhedron will inherit the space dimension of `cs`.

int ppl_new_C_Polyhedron_recycle_Congruence_System (ppl_Polyhedron_t *pph, ppl_Congruence_System_t cs) [related] Builds a new C polyhedron recycling the system of congruences *cs* and writes a handle for the newly created polyhedron at address *pph*.

The new polyhedron will inherit the space dimension of *cs*.

Warning

This function modifies the congruence system referenced by *cs* : upon return, no assumption can be made on its value.

int ppl_new_NNC_Polyhedron_from_NNC_Polyhedron_with_complexity (ppl_Polyhedron_t *pph, ppl_const_Polyhedron_t ph, int complexity) [related] Builds an NNC polyhedron that is a copy of *ph*; writes a handle for the newly created polyhedron at address *pph*.

Note

The complexity argument is ignored.

int ppl_new_NNC_Polyhedron_from_Constraint_System (ppl_Polyhedron_t *pph, ppl_const_Constraint_System_t cs) [related] Builds a new NNC polyhedron from the system of constraints *cs* and writes a handle for the newly created polyhedron at address *pph*.

The new polyhedron will inherit the space dimension of *cs*.

int ppl_new_NNC_Polyhedron_recycle_Constraint_System (ppl_Polyhedron_t *pph, ppl_Constraint_System_t cs) [related] Builds a new NNC polyhedron recycling the system of constraints *cs* and writes a handle for the newly created polyhedron at address *pph*.

The new polyhedron will inherit the space dimension of *cs*.

Warning

This function modifies the constraint system referenced by *cs* : upon return, no assumption can be made on its value.

int ppl_new_NNC_Polyhedron_from_Congruence_System (ppl_Polyhedron_t *pph, ppl_const_Congruence_System_t cs) [related] Builds a new NNC polyhedron from the system of congruences *cs* and writes a handle for the newly created polyhedron at address *pph*.

The new polyhedron will inherit the space dimension of *cs*.

int ppl_new_NNC_Polyhedron_recycle_Congruence_System (ppl_Polyhedron_t *pph, ppl_Congruence_System_t cs) [related] Builds a new NNC polyhedron recycling the system of congruences *cs* and writes a handle for the newly created polyhedron at address *pph*.

The new polyhedron will inherit the space dimension of *cs*.

Warning

This function modifies the congruence system referenced by *cs* : upon return, no assumption can be made on its value.

int ppl_new_C_Polyhedron_from_NNC_Polyhedron_with_complexity (ppl_Polyhedron_t *pph, ppl_const_Polyhedron_t ph, int complexity) [related] Builds a C polyhedron that approximates NNC_Polyhedron ph, using an algorithm whose complexity does not exceed complexity; writes a handle for the newly created polyhedron at address pph.

Note

The complexity argument, which can take values PPL_COMPLEXITY_CLASS_POLYNOMIAL, PPL_COMPLEXITY_CLASS_SIMPLEX and PPL_COMPLEXITY_CLASS_ANY, is ignored since the exact constructor has polynomial complexity.

int ppl_new_NNC_Polyhedron_from_C_Polyhedron_with_complexity (ppl_Polyhedron_t *pph, ppl_const_Polyhedron_t ph, int complexity) [related] Builds an NNC polyhedron that approximates C_Polyhedron ph, using an algorithm whose complexity does not exceed complexity; writes a handle for the newly created polyhedron at address pph.

Note

The complexity argument, which can take values PPL_COMPLEXITY_CLASS_POLYNOMIAL, PPL_COMPLEXITY_CLASS_SIMPLEX and PPL_COMPLEXITY_CLASS_ANY, is ignored since the exact constructor has polynomial complexity.

int ppl_Polyhedron_relation_with_Constraint (ppl_const_Polyhedron_t ph, ppl_const_Constraint_t c) [related] Checks the relation between the polyhedron ph and the constraint c.

If successful, returns a non-negative integer that is obtained as the bitwise or of the bits (chosen among PPL_POLY_CON_RELATION_IS_DISJOINT, PPL_POLY_CON_RELATION_STRICTLY_INTERSECTS, PPL_POLY_CON_RELATION_IS_INCLUDED, and PPL_POLY_CON_RELATION_SATURATES) that describe the relation between ph and c.

int ppl_Polyhedron_relation_with_Generator (ppl_const_Polyhedron_t ph, ppl_const_Generator_t g) [related] Checks the relation between the polyhedron ph and the generator g.

If successful, returns a non-negative integer that is obtained as the bitwise or of the bits (only PPL_POLY_GEN_RELATION_SUBSUMES, at present) that describe the relation between ph and g.

int ppl_Polyhedron_maximize_with_point (ppl_const_Polyhedron_t ph, ppl_const_Linear_Expression_t le, ppl_Coefficient_t sup_n, ppl_Coefficient_t sup_d, int *pmaximum, ppl_Generator_t point) [related] Returns a positive integer if ph is not empty and le is bounded from above in ph, in which case the supremum value and a point where le reaches it are computed.

Parameters

<i>ph</i>	The polyhedron constraining le;
<i>le</i>	The linear expression to be maximized subject to ph;
<i>sup_n</i>	Will be assigned the numerator of the supremum value;
<i>sup_d</i>	Will be assigned the denominator of the supremum value;
<i>pmaximum</i>	Will store 1 in this location if the supremum is also the maximum, will store 0 otherwise;
<i>point</i>	Will be assigned the point or closure point where le reaches the extremum value.

If ph is empty or le is not bounded from above, 0 will be returned and sup_n, sup_d, *pmaximum and point will be left untouched.

int ppl_Polyhedron_minimize_with_point (ppl_const_Polyhedron_t ph, ppl_const_Linear_Expression_t le, ppl_Coefficient_t inf_n, ppl_Coefficient_t inf_d, int *pminimum, ppl_Generator_t point) [related] Returns a positive integer if ph is not empty and le is bounded from below in ph, in which case the infimum value and a point where le reaches it are computed.

Parameters

<i>ph</i>	The polyhedron constraining <i>le</i> ;
<i>le</i>	The linear expression to be minimized subject to <i>ph</i> ;
<i>inf_n</i>	Will be assigned the numerator of the infimum value;
<i>inf_d</i>	Will be assigned the denominator of the infimum value;
<i>pminimum</i>	Will store 1 in this location if the infimum is also the minimum, will store 0 otherwise;
<i>point</i>	Will be assigned the point or closure point where <i>le</i> reaches the extremum value.

If *ph* is empty or *le* is not bounded from below, 0 will be returned and *sup_n*, *sup_d*, **pmaximum* and *point* will be left untouched.

int ppl.Polyhedron.equals.Polyhedron (ppl.const.Polyhedron.t x, ppl.const.Polyhedron.t y) [related]
Returns a positive integer if *x* and *y* are the same polyhedron; returns 0 if they are different.

Note that *x* and *y* may be topology- and/or dimension-incompatible polyhedra: in those cases, the value 0 is returned.

int ppl.Polyhedron.add_recycled_constraints (ppl.Polyhedron.t ph, ppl.Constraint_System.t cs) [related] Adds the system of constraints *cs* to the system of constraints of *ph*.

Warning

This function modifies the constraint system referenced by *cs*: upon return, no assumption can be made on its value.

int ppl.Polyhedron.add_recycled_congruences (ppl.Polyhedron.t ph, ppl.Congruence_System.t cs) [related] Adds the system of congruences *cs* to the polyhedron *ph*.

Warning

This function modifies the congruence system referenced by *cs*: upon return, no assumption can be made on its value.

int ppl.Polyhedron.upper_bound_assign (ppl.Polyhedron.t x, ppl.const.Polyhedron.t y) [related]
Assigns to *x* an upper bound of *x* and *y*.

For the domain of polyhedra, this is the same as `ppl.Polyhedron.poly_hull_assign(x, y)`.

int ppl.Polyhedron.affine_image (ppl.Polyhedron.t ph, ppl.dimension_type var, ppl.const.Linear_↔_Expression.t le, ppl.const.Coefficient.t d) [related] Transforms the polyhedron *ph*, assigning an affine expression to the specified variable.

Parameters

<i>ph</i>	The polyhedron that is transformed;
<i>var</i>	The variable to which the affine expression is assigned;
<i>le</i>	The numerator of the affine expression;
<i>d</i>	The denominator of the affine expression.

int ppl.Polyhedron.affine_preimage (ppl.Polyhedron.t ph, ppl.dimension_type var, ppl.const_↔_Linear_Expression.t le, ppl.const.Coefficient.t d) [related] Transforms the polyhedron *ph*, substituting an affine expression to the specified variable.

Parameters

<i>ph</i>	The polyhedron that is transformed;
<i>var</i>	The variable to which the affine expression is substituted;
<i>le</i>	The numerator of the affine expression;
<i>d</i>	The denominator of the affine expression.

**int ppl_Polyhedron_bounded_affine_image (ppl_Polyhedron_t *ph*, ppl_dimension_type *var*, ppl_↔
const_Linear_Expression_t *lb*, ppl_const_Linear_Expression_t *ub*, ppl_const_Coefficient_t *d*) [related]**

Assigns to *ph* the image of *ph* with respect to the *generalized affine transfer relation* $\frac{lb}{d} \leq \text{var}' \leq \frac{ub}{d}$.

Parameters

<i>ph</i>	The polyhedron that is transformed;
<i>var</i>	The variable bounded by the generalized affine transfer relation;
<i>lb</i>	The numerator of the lower bounding affine expression;
<i>ub</i>	The numerator of the upper bounding affine expression;
<i>d</i>	The (common) denominator of the lower and upper bounding affine expressions.

**int ppl_Polyhedron_bounded_affine_preimage (ppl_Polyhedron_t *ph*, ppl_dimension_type *var*, ppl_↔
const_Linear_Expression_t *lb*, ppl_const_Linear_Expression_t *ub*, ppl_const_Coefficient_t *d*) [related]**

Assigns to *ph* the preimage of *ph* with respect to the *generalized affine transfer relation* $\frac{lb}{d} \leq \text{var}' \leq \frac{ub}{d}$.

Parameters

<i>ph</i>	The polyhedron that is transformed;
<i>var</i>	The variable bounded by the generalized affine transfer relation;
<i>lb</i>	The numerator of the lower bounding affine expression;
<i>ub</i>	The numerator of the upper bounding affine expression;
<i>d</i>	The (common) denominator of the lower and upper bounding affine expressions.

**int ppl_Polyhedron_generalized_affine_image (ppl_Polyhedron_t *ph*, ppl_dimension_type *var*, enum
ppl_enum_Constraint_Type *relsym*, ppl_const_Linear_Expression_t *le*, ppl_const_Coefficient_t *d*)**

[related] Assigns to *ph* the image of *ph* with respect to the *generalized affine transfer relation* $\text{var}' \bowtie \frac{le}{d}$, where \bowtie is the relation symbol encoded by *relsym*.

Parameters

<i>ph</i>	The polyhedron that is transformed;
<i>var</i>	The left hand side variable of the generalized affine transfer relation;
<i>relsym</i>	The relation symbol;
<i>le</i>	The numerator of the right hand side affine expression;
<i>d</i>	The denominator of the right hand side affine expression.

**int ppl_Polyhedron_generalized_affine_preimage (ppl_Polyhedron_t *ph*, ppl_dimension_type *var*,
enum ppl_enum_Constraint_Type *relsym*, ppl_const_Linear_Expression_t *le*, ppl_const_Coefficient_↔
t *d*) [related]**

Assigns to *ph* the preimage of *ph* with respect to the *generalized affine transfer relation* $\text{var}' \bowtie \frac{le}{d}$, where \bowtie is the relation symbol encoded by *relsym*.

Parameters

<i>ph</i>	The polyhedron that is transformed;
<i>var</i>	The left hand side variable of the generalized affine transfer relation;
<i>relsym</i>	The relation symbol;
<i>le</i>	The numerator of the right hand side affine expression;
<i>d</i>	The denominator of the right hand side affine expression.

int ppl_Polyhedron_generalized_affine_image_lhs_rhs (ppl_Polyhedron_t *ph*, ppl_const_Linear_Expression_t *lhs*, enum ppl_enum_Constraint_Type *relsym*, ppl_const_Linear_Expression_t *rhs*) **[related]** Assigns to *ph* the image of *ph* with respect to the *generalized affine transfer relation* $lhs' \bowtie rhs$, where \bowtie is the relation symbol encoded by *relsym*.

Parameters

<i>ph</i>	The polyhedron that is transformed;
<i>lhs</i>	The left hand side affine expression;
<i>relsym</i>	The relation symbol;
<i>rhs</i>	The right hand side affine expression.

int ppl_Polyhedron_generalized_affine_preimage_lhs_rhs (ppl_Polyhedron_t *ph*, ppl_const_Linear_Expression_t *lhs*, enum ppl_enum_Constraint_Type *relsym*, ppl_const_Linear_Expression_t *rhs*) **[related]** Assigns to *ph* the preimage of *ph* with respect to the *generalized affine transfer relation* $lhs' \bowtie rhs$, where \bowtie is the relation symbol encoded by *relsym*.

Parameters

<i>ph</i>	The polyhedron that is transformed;
<i>lhs</i>	The left hand side affine expression;
<i>relsym</i>	The relation symbol;
<i>rhs</i>	The right hand side affine expression.

int ppl_Polyhedron_map_space_dimensions (ppl_Polyhedron_t *ph*, ppl_dimension_type *maps*[], size_t *n*) **[related]** Remaps the dimensions of the vector space according to a *partial function*. This function is specified by means of the *maps* array, which has *n* entries.

The partial function is defined on dimension *i* if $i < n$ and $maps[i] \neq ppl_not_a_dimension$; otherwise it is undefined on dimension *i*. If the function is defined on dimension *i*, then dimension *i* is mapped onto dimension $maps[i]$.

The result is undefined if *maps* does not encode a partial function with the properties described in the *specification of the mapping operator*.

int ppl_new_C_Polyhedron_from_Generator_System (ppl_Polyhedron_t * *pph*, ppl_const_Generator_System_t *gs*) **[related]** Builds a new C polyhedron from the system of generators *gs* and writes a handle for the newly created polyhedron at address *pph*.

The new polyhedron will inherit the space dimension of *gs*.

int ppl_new_C_Polyhedron_recycle_Generator_System (ppl_Polyhedron_t * *pph*, ppl_Generator_System_t *gs*) **[related]** Builds a new C polyhedron recycling the system of generators *gs* and writes a handle for the newly created polyhedron at address *pph*.

The new polyhedron will inherit the space dimension of *gs*.

Warning

This function modifies the generator system referenced by *gs*: upon return, no assumption can be made on its value.

int ppl_new_NNC_Polyhedron_from_Generator_System (ppl_Polyhedron_t *pph, ppl_const_Generator_System_t gs) [related] Builds a new NNC polyhedron from the system of generators *gs* and writes a handle for the newly created polyhedron at address *pph*.

The new polyhedron will inherit the space dimension of *gs*.

int ppl_new_NNC_Polyhedron_recycle_Generator_System (ppl_Polyhedron_t *pph, ppl_Generator_System_t gs) [related] Builds a new NNC polyhedron recycling the system of generators *gs* and writes a handle for the newly created polyhedron at address *pph*.

The new polyhedron will inherit the space dimension of *gs*.

Warning

This function modifies the generator system referenced by *gs*: upon return, no assumption can be made on its value.

int ppl_Polyhedron_add_recycled_generators (ppl_Polyhedron_t ph, ppl_Generator_System_t gs) [related] Adds the system of generators *gs* to the system of generators of *ph*.

Warning

This function modifies the generator system referenced by *gs*: upon return, no assumption can be made on its value.

int wrap_assign (ppl_Polyhedron_t ph, ppl_dimension_type ds[], size_t n, ppl_enum_Bounded_Integer_Type_Width w, ppl_enum_Bounded_Integer_Type_Representation r, ppl_enum_Bounded_Integer_Type_Overflow o, const ppl_const_Constraint_System_t *pcs, unsigned complexity_threshold, int wrap_individually) [related] Assigns to *ph* the polyhedron obtained from *ph* by "wrapping" the vector space defined by the first *n* space dimensions in *ds*[].

Parameters

<i>ph</i>	The polyhedron that is transformed;
<i>ds[]</i>	Specifies the space dimensions to be wrapped.
<i>n</i>	The first <i>n</i> space dimensions in the array <i>ds</i> [] will be wrapped.
<i>w</i>	The width of the bounded integer type corresponding to all the dimensions to be wrapped.
<i>r</i>	The representation of the bounded integer type corresponding to all the dimensions to be wrapped.
<i>o</i>	The overflow behavior of the bounded integer type corresponding to all the dimensions to be wrapped.
<i>pcs</i>	Possibly null pointer to a constraint system whose space dimensions are the first <i>n</i> dimensions in <i>ds</i> [] . If <i>*pcs</i> depends on variables not in <i>vars</i> , the behavior is undefined. When non-null, the constraint system is assumed to represent the conditional or looping construct guard with respect to which wrapping is performed. Since wrapping requires the computation of upper bounds and due to non-distributivity of constraint refinement over upper bounds, passing a constraint system in this way can be more precise than refining the result of the wrapping operation with the constraints in <i>cs</i> .

<i>complexity_↔ threshold</i>	A precision parameter where higher values result in possibly improved precision.
<i>wrap_↔ individually</i>	Non-zero if the dimensions should be wrapped individually (something that results in much greater efficiency to the detriment of precision).

The documentation for this interface was generated from the following file:

- C_interface.dox

Index

C Language Interface, 17

Error Handling, 20

- PPL_ARITHMETIC_OVERFLOW, 20
- PPL_ERROR_DOMAIN_ERROR, 20
- PPL_ERROR_INTERNAL_ERROR, 20
- PPL_ERROR_INVALID_ARGUMENT, 20
- PPL_ERROR_LENGTH_ERROR, 20
- PPL_ERROR_LOGIC_ERROR, 20
- PPL_ERROR_OUT_OF_MEMORY, 20
- PPL_ERROR_UNEXPECTED_ERROR, 20
- PPL_ERROR_UNKNOWN_STANDARD_EXCEPTION, 20
- PPL_STDIO_ERROR, 20
- PPL_TIMEOUT_EXCEPTION, 20
- ppl_enum_error_code, 20
- ppl_set_error_handler, 21

Library Datatypes, 24

- PPL_BITS_128, 29
- PPL_BITS_16, 29
- PPL_BITS_32, 29
- PPL_BITS_64, 29
- PPL_BITS_8, 29
- PPL_CONSTRAINT_TYPE_EQUAL, 28
- PPL_CONSTRAINT_TYPE_GREATER_OR_EQUAL, 28
- PPL_CONSTRAINT_TYPE_GREATER_THAN, 28
- PPL_CONSTRAINT_TYPE_LESS_OR_EQUAL, 28
- PPL_CONSTRAINT_TYPE_LESS_THAN, 28
- PPL_GENERATOR_TYPE_CLOSURE_POINT, 28
- PPL_GENERATOR_TYPE_LINE, 28
- PPL_GENERATOR_TYPE_POINT, 28
- PPL_GENERATOR_TYPE_RAY, 28
- PPL_GRID_GENERATOR_TYPE_LINE, 28
- PPL_GRID_GENERATOR_TYPE_PARAMETER, 28
- PPL_GRID_GENERATOR_TYPE_POINT, 28
- PPL_OVERFLOW_IMPOSSIBLE, 29
- PPL_OVERFLOW_UNDEFINED, 29
- PPL_OVERFLOW_WRAPS, 29
- PPL_SIGNED_2_COMPLEMENT, 29
- PPL_UNSIGNED, 29
- ppl_enum_Bounded_Integer_Type_Overflow, 29
- ppl_enum_Bounded_Integer_Type_Representation, 29
- ppl_enum_Bounded_Integer_Type_Width, 28
- ppl_enum_Constraint_Type, 28

- ppl_enum_Generator_Type, 28
- ppl_enum_Grid_Generator_Type, 28
- ppl_io_variable_output_function_type, 28
- ppl_io_wrap_string, 29

Library Initialization and Finalization, 18

- ppl_finalize, 18
- ppl_initialize, 18
- ppl_restore_pre_PPL_rounding, 18
- ppl_set_irrational_precision, 18
- ppl_set_rounding_for_PPL, 18

- PPL_ARITHMETIC_OVERFLOW
 - Error Handling, 20
- PPL_BITS_128
 - Library Datatypes, 29
- PPL_BITS_16
 - Library Datatypes, 29
- PPL_BITS_32
 - Library Datatypes, 29
- PPL_BITS_64
 - Library Datatypes, 29
- PPL_BITS_8
 - Library Datatypes, 29
- PPL_CONSTRAINT_TYPE_EQUAL
 - Library Datatypes, 28
- PPL_CONSTRAINT_TYPE_GREATER_OR_EQUAL
 - Library Datatypes, 28
- PPL_CONSTRAINT_TYPE_GREATER_THAN
 - Library Datatypes, 28
- PPL_CONSTRAINT_TYPE_LESS_OR_EQUAL
 - Library Datatypes, 28
- PPL_CONSTRAINT_TYPE_LESS_THAN
 - Library Datatypes, 28
- PPL_ERROR_DOMAIN_ERROR
 - Error Handling, 20
- PPL_ERROR_INTERNAL_ERROR
 - Error Handling, 20
- PPL_ERROR_INVALID_ARGUMENT
 - Error Handling, 20
- PPL_ERROR_LENGTH_ERROR
 - Error Handling, 20
- PPL_ERROR_LOGIC_ERROR
 - Error Handling, 20
- PPL_ERROR_OUT_OF_MEMORY
 - Error Handling, 20
- PPL_ERROR_UNEXPECTED_ERROR
 - Error Handling, 20
- PPL_ERROR_UNKNOWN_STANDARD_EXCEPTION
 - Error Handling, 20

PPL_GENERATOR_TYPE_CLOSURE_POINT
Library Datatypes, 28
PPL_GENERATOR_TYPE_LINE
Library Datatypes, 28
PPL_GENERATOR_TYPE_POINT
Library Datatypes, 28
PPL_GENERATOR_TYPE_RAY
Library Datatypes, 28
PPL_GRID_GENERATOR_TYPE_LINE
Library Datatypes, 28
PPL_GRID_GENERATOR_TYPE_PARAMETER
Library Datatypes, 28
PPL_GRID_GENERATOR_TYPE_POINT
Library Datatypes, 28
PPL_OVERFLOW_IMPOSSIBLE
Library Datatypes, 29
PPL_OVERFLOW_UNDEFINED
Library Datatypes, 29
PPL_OVERFLOW_WRAPS
Library Datatypes, 29
PPL_SIGNED_2_COMPLEMENT
Library Datatypes, 29
PPL_STDIO_ERROR
Error Handling, 20
PPL_TIMEOUT_EXCEPTION
Error Handling, 20
PPL_UNSIGNED
Library Datatypes, 29
PPL_VERSION
Version Checking, 19
ppl_Artificial_Parameter_Sequence_const_iterator↔
tag, 31
ppl_Artificial_Parameter_tag, 31
ppl_Coefficient_tag, 32
ppl_Congruence_System_const_iterator_tag, 33
ppl_Congruence_System_tag, 34
ppl_Congruence_tag, 36
ppl_Constraint_System_const_iterator_tag, 37
ppl_Constraint_System_tag, 37
ppl_Constraint_tag, 39
ppl_Generator_System_const_iterator_tag, 40
ppl_Generator_System_tag, 41
ppl_Generator_tag, 42
ppl_Grid_Generator_System_const_iterator_tag, 43
ppl_Grid_Generator_System_tag, 44
ppl_Grid_Generator_tag, 46
ppl_Linear_Expression_tag, 47
ppl_MIP_Problem_evaluate_objective_function
ppl_MIP_Problem_tag, 51
ppl_MIP_Problem_optimal_value
ppl_MIP_Problem_tag, 53
ppl_MIP_Problem_solve
ppl_MIP_Problem_tag, 51
ppl_MIP_Problem_tag, 49
ppl_MIP_Problem_evaluate_objective_function,
51
ppl_MIP_Problem_optimal_value, 53
ppl_MIP_Problem_solve, 51
ppl_PIP_Decision_Node_tag, 53
ppl_PIP_Problem_add_space_dimensions_and_embed
ppl_PIP_Problem_tag, 56
ppl_PIP_Problem_solve
ppl_PIP_Problem_tag, 56
ppl_PIP_Problem_space_dimension
ppl_PIP_Problem_tag, 56
ppl_PIP_Problem_tag, 54
ppl_PIP_Problem_add_space_dimensions_and↔
_embed, 56
ppl_PIP_Problem_solve, 56
ppl_PIP_Problem_space_dimension, 56
ppl_PIP_Solution_Node_get_parametric_values
ppl_PIP_Solution_Node_tag, 57
ppl_PIP_Solution_Node_tag, 57
ppl_PIP_Solution_Node_get_parametric_values, 57
ppl_PIP_Tree_Node_tag, 58
ppl_Pointset_Powerset_C_Polyhedron_const_iterator↔
_dereference
ppl_Pointset_Powerset_C_Polyhedron_const_iterator↔
_tag, 60
ppl_Pointset_Powerset_C_Polyhedron_const_iterator↔
_tag, 59
ppl_Pointset_Powerset_C_Polyhedron_const_iterator↔
_dereference, 60
ppl_Pointset_Powerset_C_Polyhedron_iterator_dereference
ppl_Pointset_Powerset_C_Polyhedron_iterator↔
_tag, 61
ppl_Pointset_Powerset_C_Polyhedron_iterator_tag, 60
ppl_Pointset_Powerset_C_Polyhedron_iterator↔
_dereference, 61
ppl_Pointset_Powerset_C_Polyhedron_size
ppl_Pointset_Powerset_C_Polyhedron_tag, 62
ppl_Pointset_Powerset_C_Polyhedron_tag, 61
ppl_Pointset_Powerset_C_Polyhedron_size, 62
ppl_Polyhedron_add_recycled_congruences
ppl_Polyhedron_tag, 73
ppl_Polyhedron_add_recycled_constraints
ppl_Polyhedron_tag, 73
ppl_Polyhedron_add_recycled_generators
ppl_Polyhedron_tag, 76
ppl_Polyhedron_affine_image
ppl_Polyhedron_tag, 73
ppl_Polyhedron_affine_preimage
ppl_Polyhedron_tag, 73
ppl_Polyhedron_bounded_affine_image
ppl_Polyhedron_tag, 74
ppl_Polyhedron_bounded_affine_preimage
ppl_Polyhedron_tag, 74
ppl_Polyhedron_equals_Polyhedron

[ppl.Polyhedron_tag](#), [73](#)
[ppl.Polyhedron_generalized_affine_image](#)
[ppl.Polyhedron_tag](#), [74](#)
[ppl.Polyhedron_generalized_affine_image_lhs_rhs](#)
[ppl.Polyhedron_tag](#), [75](#)
[ppl.Polyhedron_generalized_affine_preimage](#)
[ppl.Polyhedron_tag](#), [74](#)
[ppl.Polyhedron_generalized_affine_preimage_lhs_rhs](#)
[ppl.Polyhedron_tag](#), [75](#)
[ppl.Polyhedron_map_space_dimensions](#)
[ppl.Polyhedron_tag](#), [75](#)
[ppl.Polyhedron_maximize_with_point](#)
[ppl.Polyhedron_tag](#), [72](#)
[ppl.Polyhedron_minimize_with_point](#)
[ppl.Polyhedron_tag](#), [72](#)
[ppl.Polyhedron_relation_with_Constraint](#)
[ppl.Polyhedron_tag](#), [72](#)
[ppl.Polyhedron_relation_with_Generator](#)
[ppl.Polyhedron_tag](#), [72](#)
[ppl.Polyhedron_tag](#), [62](#)
[ppl.Polyhedron_add_recycled_congruences](#), [73](#)
[ppl.Polyhedron_add_recycled_constraints](#), [73](#)
[ppl.Polyhedron_add_recycled_generators](#), [76](#)
[ppl.Polyhedron_affine_image](#), [73](#)
[ppl.Polyhedron_affine_preimage](#), [73](#)
[ppl.Polyhedron_bounded_affine_image](#), [74](#)
[ppl.Polyhedron_bounded_affine_preimage](#), [74](#)
[ppl.Polyhedron_equals_Polyhedron](#), [73](#)
[ppl.Polyhedron_generalized_affine_image](#), [74](#)
[ppl.Polyhedron_generalized_affine_image_lhs↔_rhs](#), [75](#)
[ppl.Polyhedron_generalized_affine_preimage](#), [74](#)
[ppl.Polyhedron_generalized_affine_preimage↔_lhs_rhs](#), [75](#)
[ppl.Polyhedron_map_space_dimensions](#), [75](#)
[ppl.Polyhedron_maximize_with_point](#), [72](#)
[ppl.Polyhedron_minimize_with_point](#), [72](#)
[ppl.Polyhedron_relation_with_Constraint](#), [72](#)
[ppl.Polyhedron_relation_with_Generator](#), [72](#)
[ppl.Polyhedron_upper_bound_assign](#), [73](#)
[ppl_new_C.Polyhedron_from_C.Polyhedron↔_with_complexity](#), [70](#)
[ppl_new_C.Polyhedron_from_Congruence_System](#), [70](#)
[ppl_new_C.Polyhedron_from_Constraint_System](#), [70](#)
[ppl_new_C.Polyhedron_from_Generator_System](#), [75](#)
[ppl_new_C.Polyhedron_from_NNC.Polyhedron↔_with_complexity](#), [71](#)
[ppl_new_C.Polyhedron_recycle_Congruence_System](#), [70](#)
[ppl_new_C.Polyhedron_recycle_Constraint_System](#), [70](#)
[ppl_new_C.Polyhedron_recycle_Generator_System](#), [75](#)
[ppl_new_NNC.Polyhedron_from_C.Polyhedron↔_with_complexity](#), [72](#)
[ppl_new_NNC.Polyhedron_from_Congruence↔_System](#), [71](#)
[ppl_new_NNC.Polyhedron_from_Constraint↔_System](#), [71](#)
[ppl_new_NNC.Polyhedron_from_Generator_System](#), [75](#)
[ppl_new_NNC.Polyhedron_from_NNC.Polyhedron↔_with_complexity](#), [71](#)
[ppl_new_NNC.Polyhedron_recycle_Congruence↔_System](#), [71](#)
[ppl_new_NNC.Polyhedron_recycle_Constraint↔_System](#), [71](#)
[ppl_new_NNC.Polyhedron_recycle_Generator↔_System](#), [76](#)
[wrap_assign](#), [76](#)
[ppl.Polyhedron_upper_bound_assign](#)
[ppl.Polyhedron_tag](#), [73](#)
[ppl.banner](#)
[Version Checking](#), [19](#)
[ppl.enum_Bounded_Integer_Type_Overflow](#)
[Library Datatypes](#), [29](#)
[ppl.enum_Bounded_Integer_Type_Representation](#)
[Library Datatypes](#), [29](#)
[ppl.enum_Bounded_Integer_Type_Width](#)
[Library Datatypes](#), [28](#)
[ppl.enum_Constraint_Type](#)
[Library Datatypes](#), [28](#)
[ppl.enum_Generator_Type](#)
[Library Datatypes](#), [28](#)
[ppl.enum_Grid_Generator_Type](#)
[Library Datatypes](#), [28](#)
[ppl.enum_error_code](#)
[Error Handling](#), [20](#)
[ppl.finalize](#)
[Library Initialization and Finalization](#), [18](#)
[ppl.initialize](#)
[Library Initialization and Finalization](#), [18](#)
[ppl.io_variable_output_function_type](#)
[Library Datatypes](#), [28](#)
[ppl.io_wrap_string](#)
[Library Datatypes](#), [29](#)
[ppl_new_C.Polyhedron_from_C.Polyhedron↔_with↔_complexity](#)
[ppl.Polyhedron_tag](#), [70](#)
[ppl_new_C.Polyhedron_from_Congruence_System](#)
[ppl.Polyhedron_tag](#), [70](#)
[ppl_new_C.Polyhedron_from_Constraint_System](#)
[ppl.Polyhedron_tag](#), [70](#)
[ppl_new_C.Polyhedron_from_Generator_System](#)
[ppl.Polyhedron_tag](#), [75](#)

- ppl_new_C_Polyhedron_from_NNC_Polyhedron_with↔
_complexity
ppl.Polyhedron_tag, 71
- ppl_new_C_Polyhedron_recycle_Congruence_System
ppl.Polyhedron_tag, 70
- ppl_new_C_Polyhedron_recycle_Constraint_System
ppl.Polyhedron_tag, 70
- ppl_new_C_Polyhedron_recycle_Generator_System
ppl.Polyhedron_tag, 75
- ppl_new_NNC_Polyhedron_from_C_Polyhedron_with↔
_complexity
ppl.Polyhedron_tag, 72
- ppl_new_NNC_Polyhedron_from_Congruence_System
ppl.Polyhedron_tag, 71
- ppl_new_NNC_Polyhedron_from_Constraint_System
ppl.Polyhedron_tag, 71
- ppl_new_NNC_Polyhedron_from_Generator_System
ppl.Polyhedron_tag, 75
- ppl_new_NNC_Polyhedron_from_NNC_Polyhedron↔
_with_complexity
ppl.Polyhedron_tag, 71
- ppl_new_NNC_Polyhedron_recycle_Congruence_System
ppl.Polyhedron_tag, 71
- ppl_new_NNC_Polyhedron_recycle_Constraint_System
ppl.Polyhedron_tag, 71
- ppl_new_NNC_Polyhedron_recycle_Generator_System
ppl.Polyhedron_tag, 76
- ppl_restore_pre_PPL_rounding
Library Initialization and Finalization, 18
- ppl_set_deterministic_timeout
Timeout Handling, 22
- ppl_set_error_handler
Error Handling, 21
- ppl_set_irrational_precision
Library Initialization and Finalization, 18
- ppl_set_rounding_for_PPL
Library Initialization and Finalization, 18
- ppl_set_timeout
Timeout Handling, 22

- Timeout Handling, 22
 - ppl_set_deterministic_timeout, 22
 - ppl_set_timeout, 22

- Version Checking, 19
 - PPL_VERSION, 19
 - ppl_banner, 19

- wrap_assign
ppl.Polyhedron_tag, 76